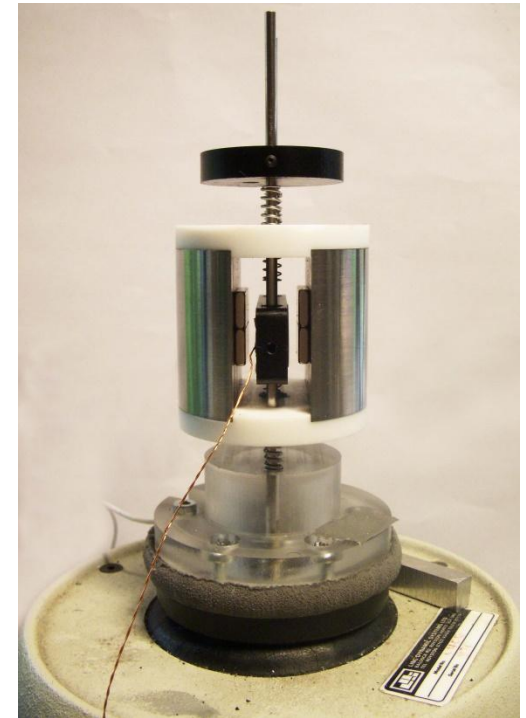


# A multiple Dof velocity amplified VEH: experimental analysis and modelling



Valeria Nico<sup>1</sup>, Elisabetta Boco<sup>1</sup>, Declan O'Donoghue<sup>1</sup>, Ronan Frizzell<sup>2</sup>, Gerard Kelly<sup>2</sup>, Jeff Punch<sup>1</sup>

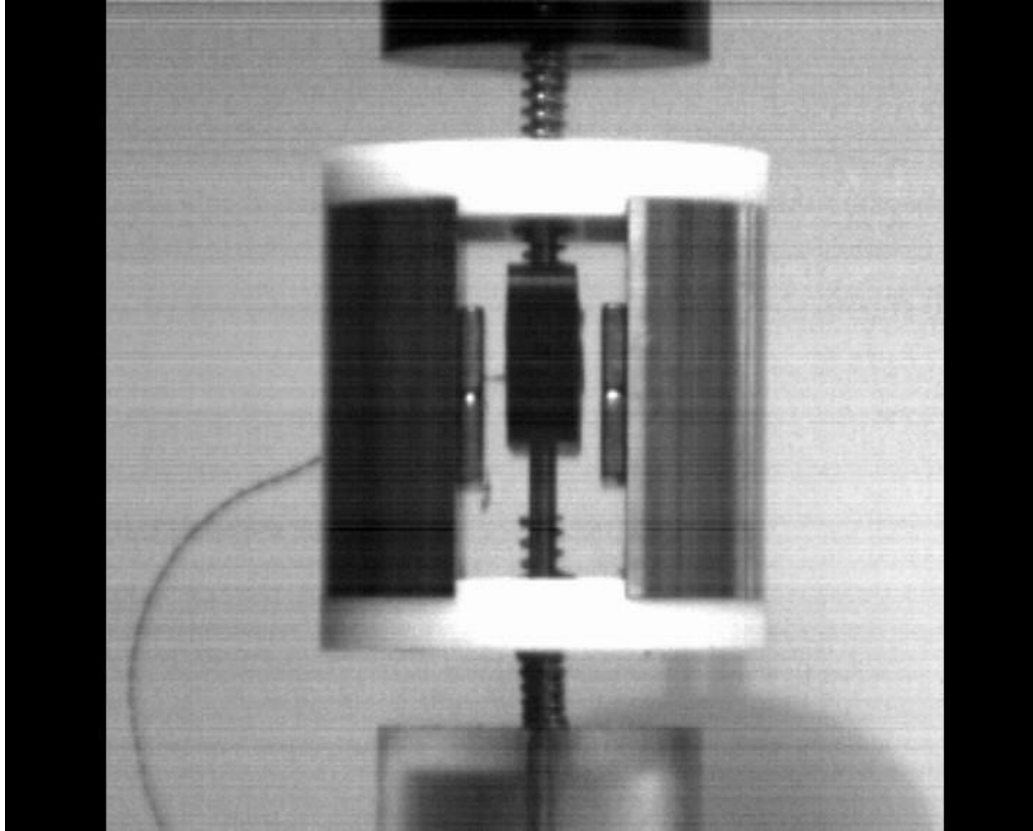
1. *CTVR, Stokes Institute, University of Limerick, Limerick, Ireland*

2. *Efficient Energy Transfer Dept., Bell Labs, Alcatel-Lucent, Dublin, Ireland*

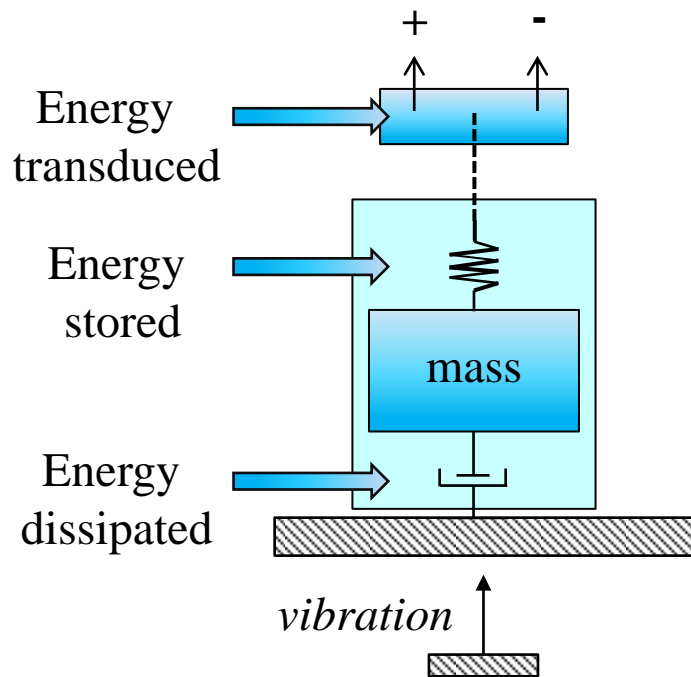
# Outline

- Vibrational Energy Harvester
- Electromagnetic Energy Harvester
- Experimental setup
- Harvester prototype results
- Theoretical model of a 2Dof harvester
- Summary and future work

# 2Dof Energy Harvester



# Vibration Energy Harvester



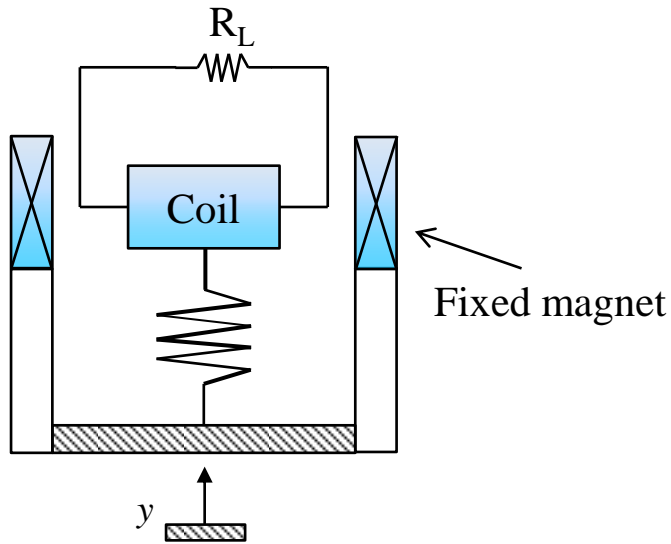
$$\left\{ \begin{aligned} m\ddot{x} &= -\frac{\partial U(x)}{\partial x} - \gamma\dot{x} - c(x, V) + \xi_z \\ \dot{V} &= F(\dot{x}, V) \end{aligned} \right.$$

Potential  $\uparrow$   $\frac{\partial U(x)}{\partial x}$       Friction  $\uparrow$   $\gamma\dot{x}$       Dissipative force  $\uparrow$   $c(x, V)$       Input force  $\uparrow$   $\xi_z$

Depend on the transduction mechanism

Linear case:  $\frac{\partial U(x)}{\partial x} = kx$

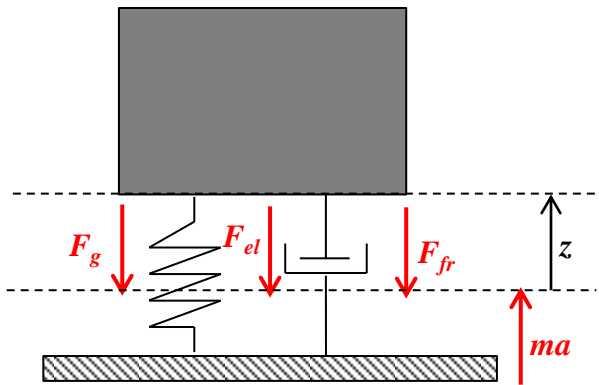
# Vibrations Harvester: electromagnetic transducer



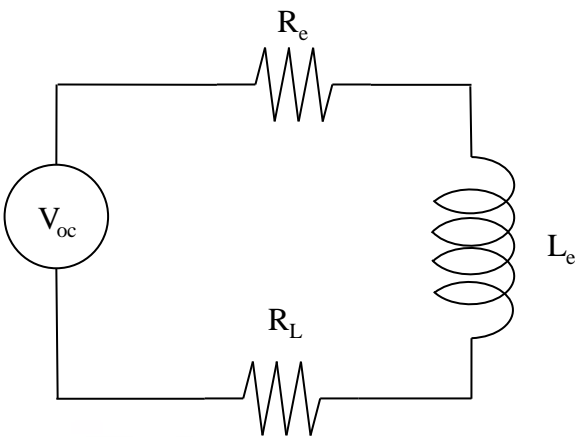
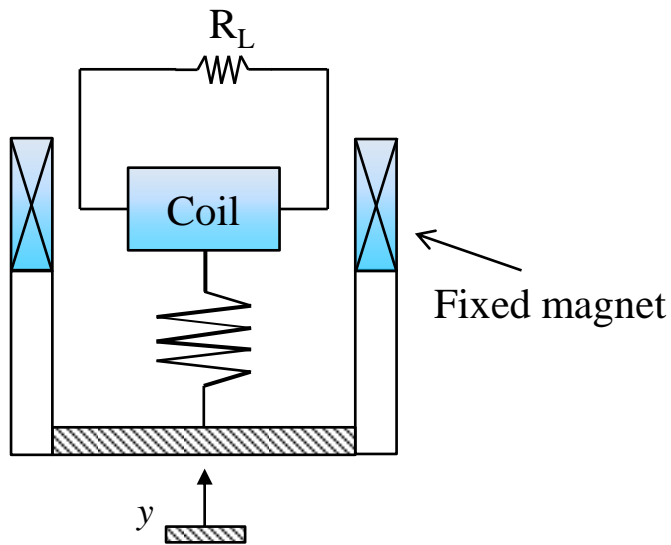
Mechanical part:

$$m\ddot{z} = F_{el} + F_{fr} - ma + F_g$$

$$m\ddot{z} = -kz - d\dot{z} - \alpha V_L - m\ddot{y} - mg$$



# Vibrations Harvester: electromagnetic transducer



Faraday's Law

$$V_{oc} = - \frac{d\Phi_B}{dt} = NBl \frac{dx}{dt}$$

$N$  = number of turns

$B$  = strength of the magnetic field

$l$  = length of the wire

$$V_L = Bl\dot{z} - R_e i - L_e \frac{di}{dt}$$

$$\dot{V}_L + V_L \left( \frac{R_L + R_e}{L_e} \right) = Bl \frac{R_L}{L_e} \dot{z}$$

$$\dot{V}_L + V_L \omega_c = \delta_c \omega_c \dot{z}$$

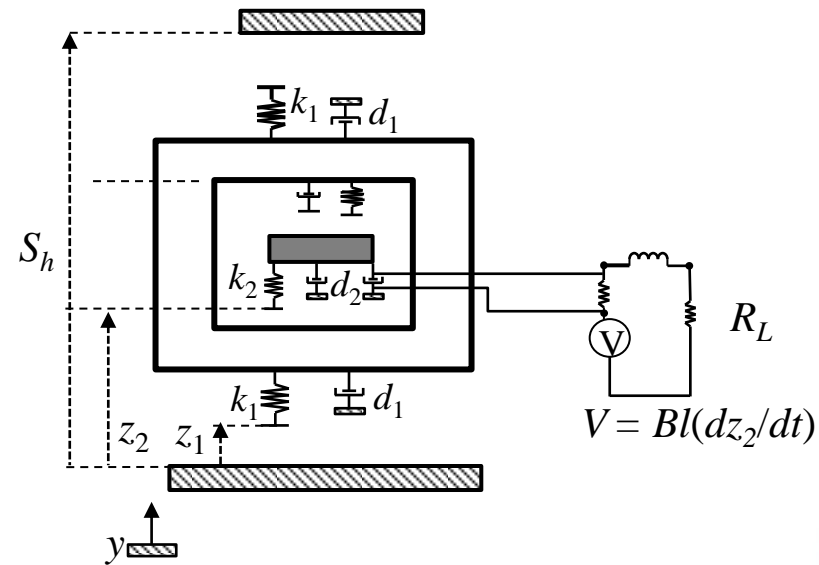
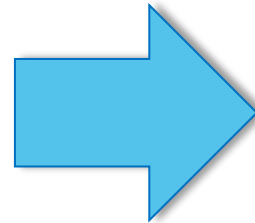
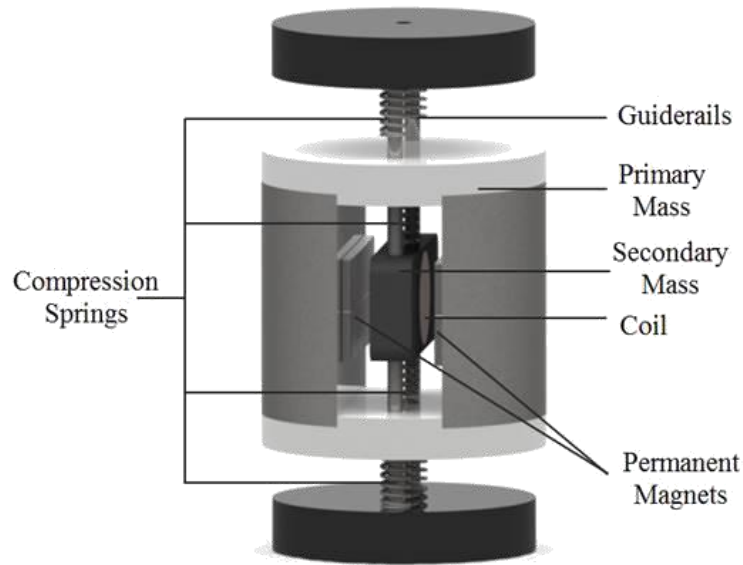
$\alpha = B_z l / R_l$  : electric coupling factor;

$\delta_c = B_z l$  : conversion factor;

$\omega_c = R_l / L_e$  : characteristic cut frequency;

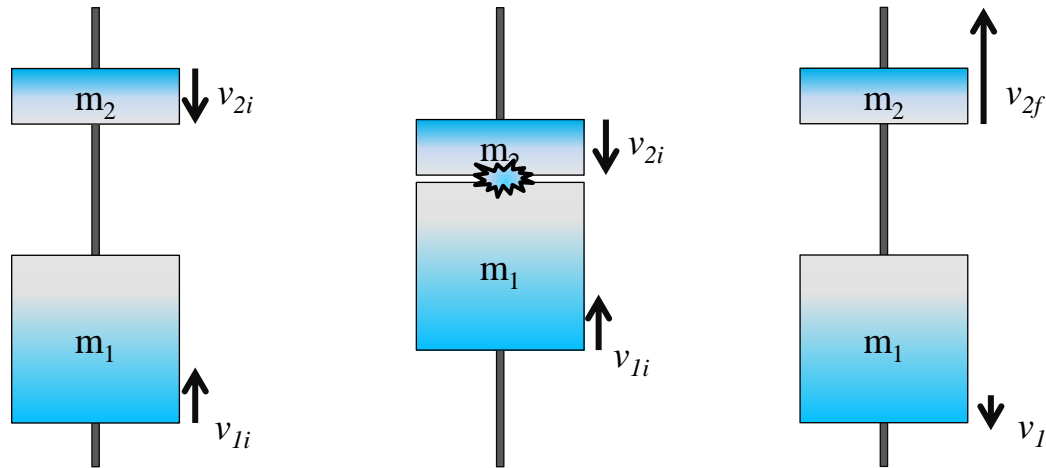
$L_e = \mu_0 N^2 \pi R^2 / h_b$  : coil inductance.

# 2Dof Energy Harvester



- Two masses connected by springs;
- A coil is embedded in the secondary mass and 4 magnets are inside the primary mass;
- Impacts between the masses and between each mass and the housing are allowed;
- Velocity of the secondary mass is increased by exploiting velocity amplification

# Velocity amplification

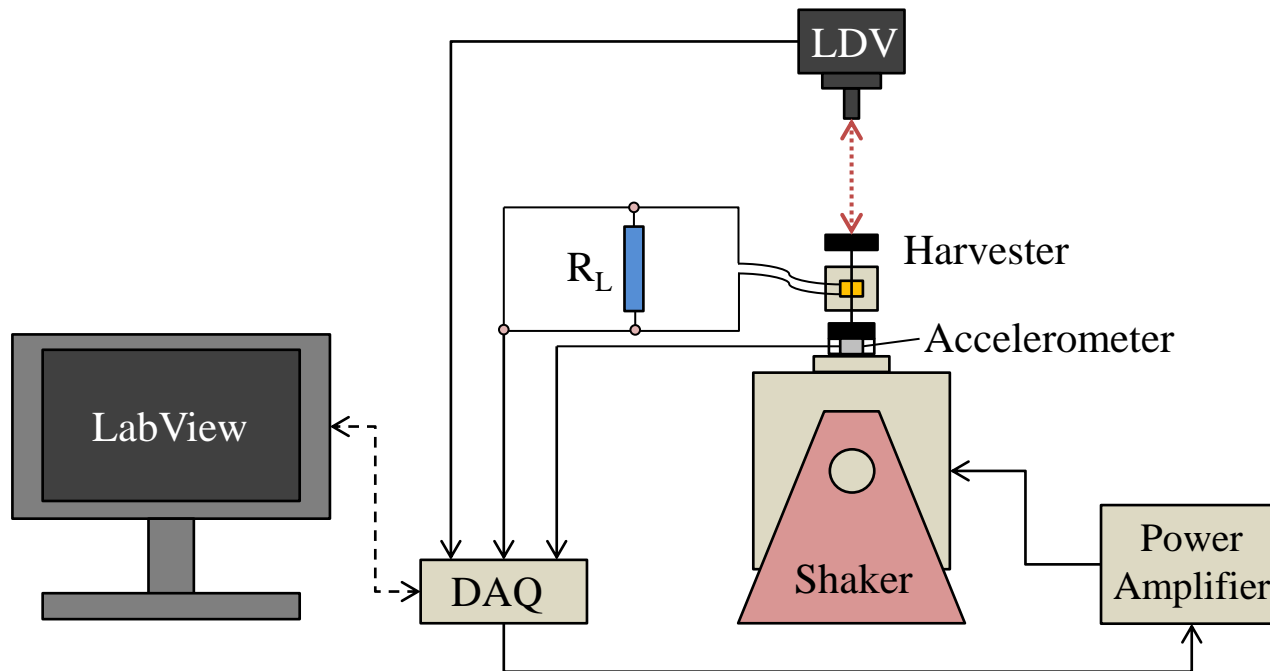


- Velocity amplification is achieved by utilizing sequential collisions in a series of free moving masses;
- The energy lost in the impact is accounted for through the coefficient of restitution;
- The coefficient of restitution,  $e$ , for the impact between  $m_1$  and  $m_2$  is defined as

$$e_{2,1} = \frac{\text{relative velocity after collision}}{\text{relative velocity before collision}} = -\frac{v_{2f} - v_{1f}}{v_{2i} - v_{1i}}$$

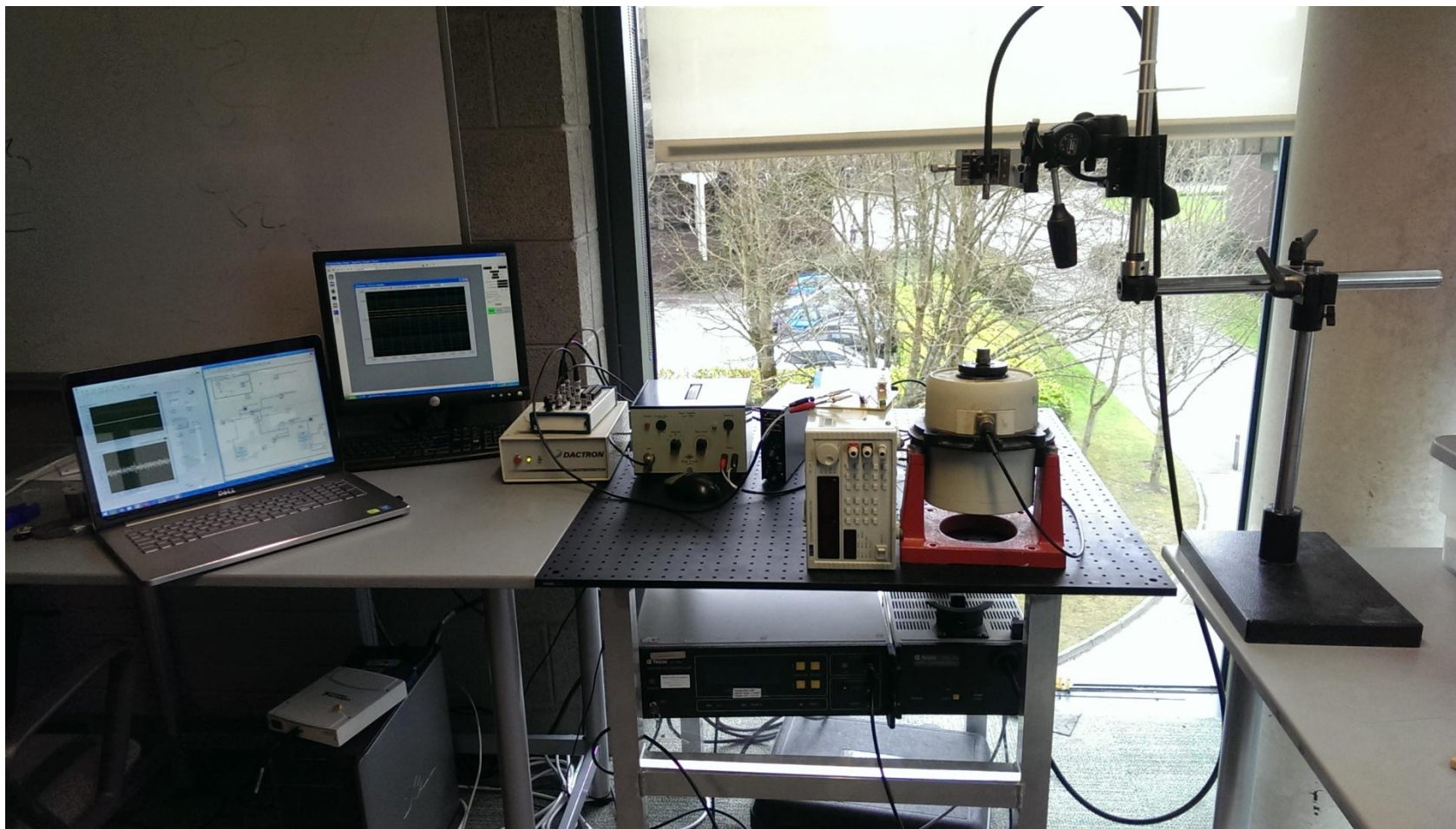


# Experimental setup

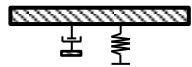
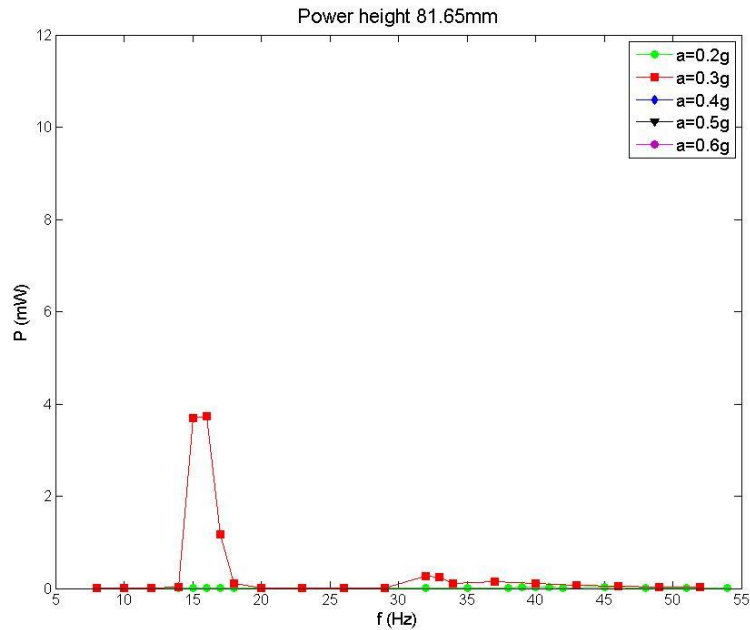


- Labview is used to supply a voltage signal to the shaker through a power amplifier;
- An accelerometer, mounted on the head of the shaker, provides a feedback control of the acceleration;
- The voltage signal of the harvester is measured across a variable load  $R_L$ .

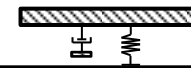
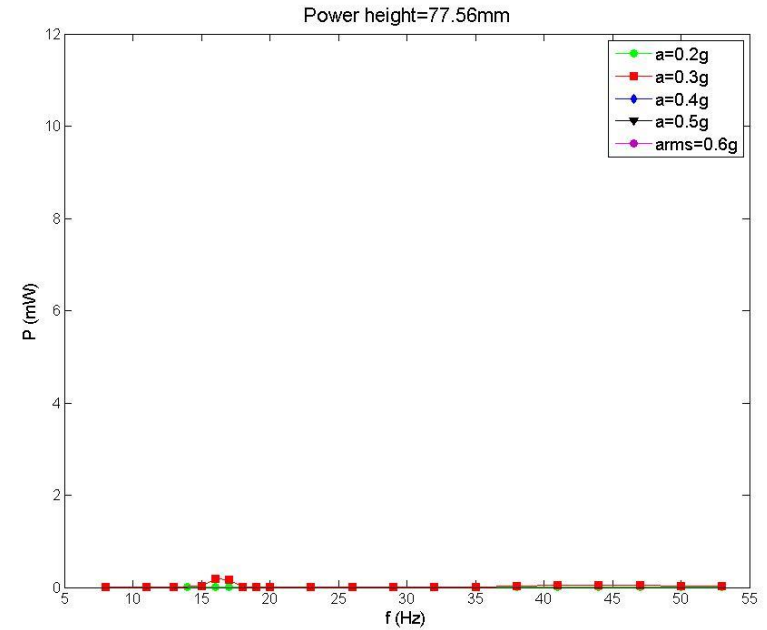
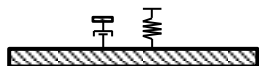
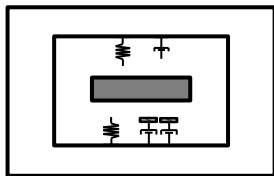
# Experimental setup



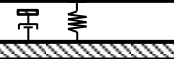
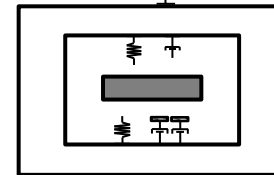
# Harvester Power Output



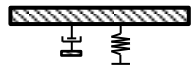
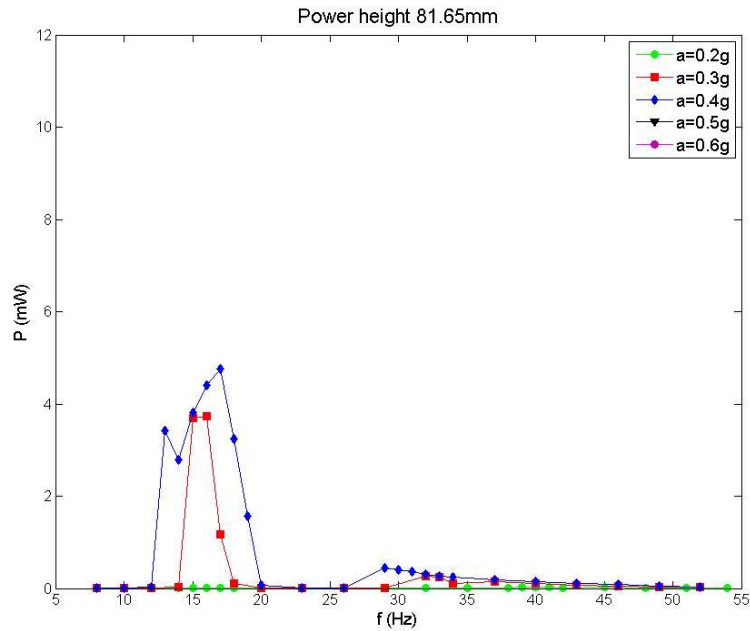
Cap height = 81.65 mm



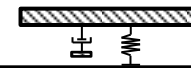
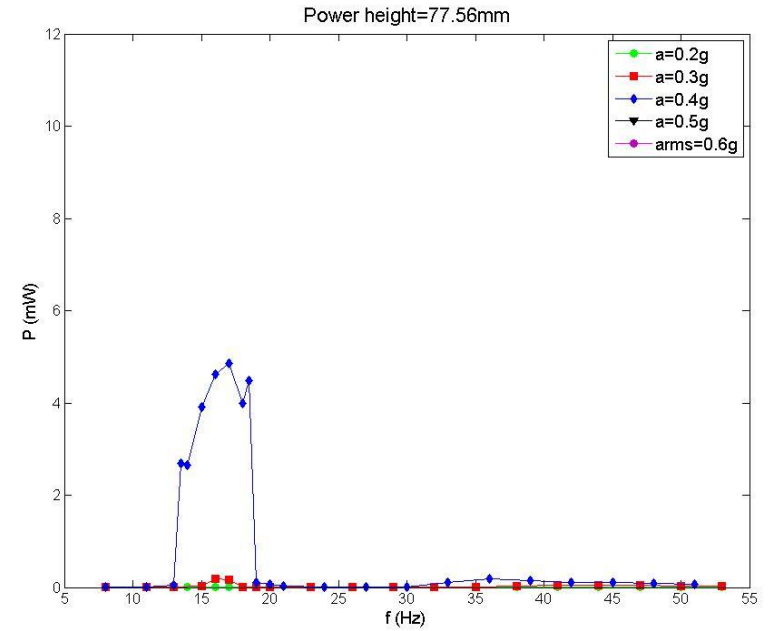
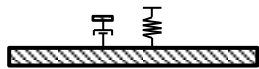
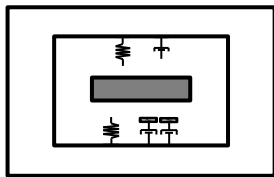
Cap height = 77.58 mm



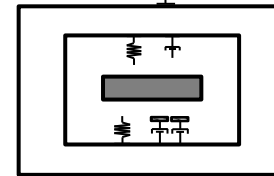
# Harvester Power Output



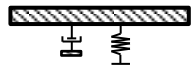
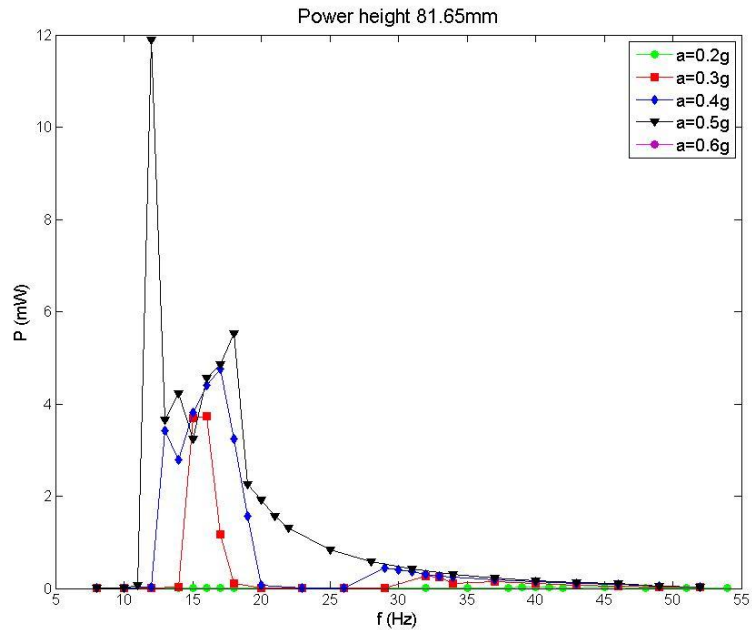
Cap height = 81.65 mm



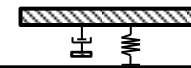
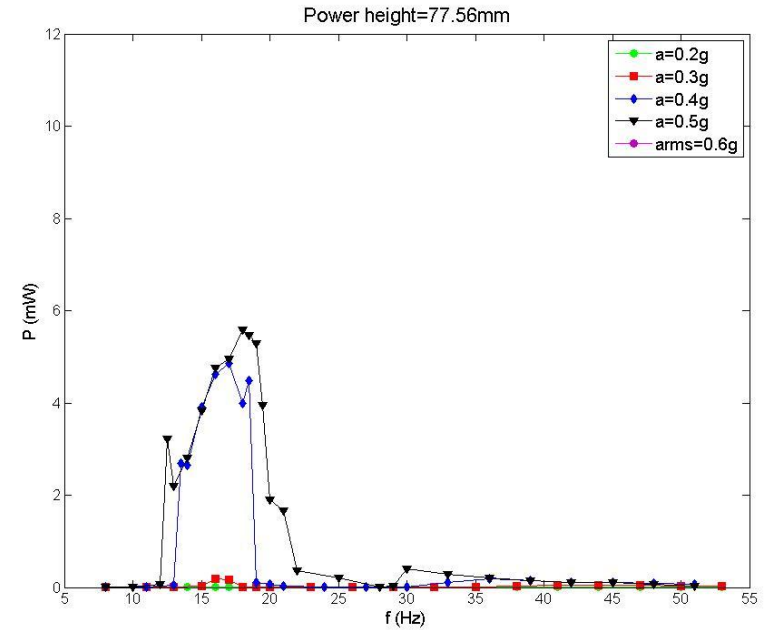
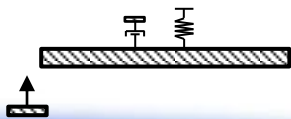
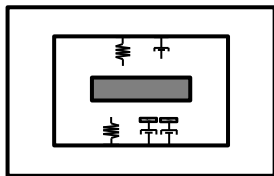
Cap height = 77.58 mm



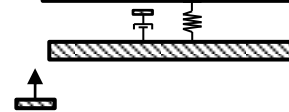
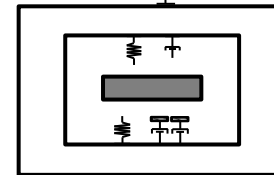
# Harvester Power Output



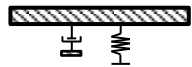
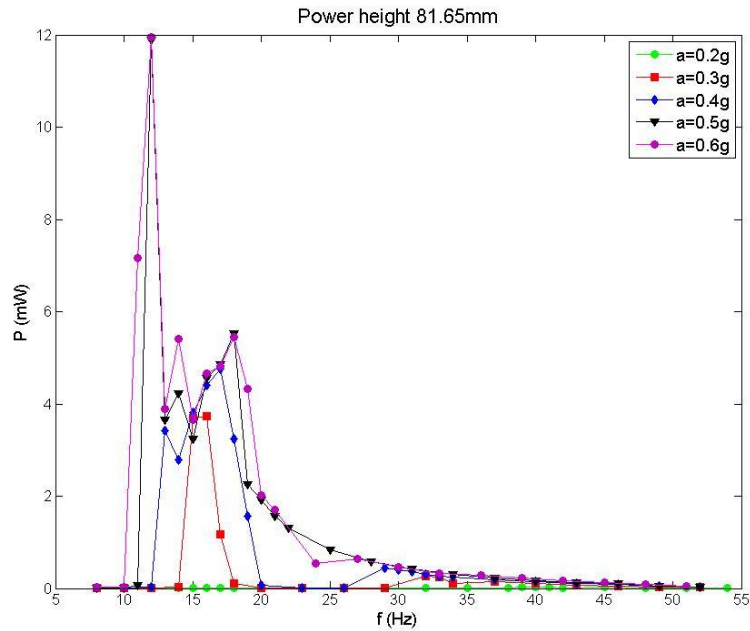
Cap height = 81.65 mm



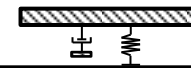
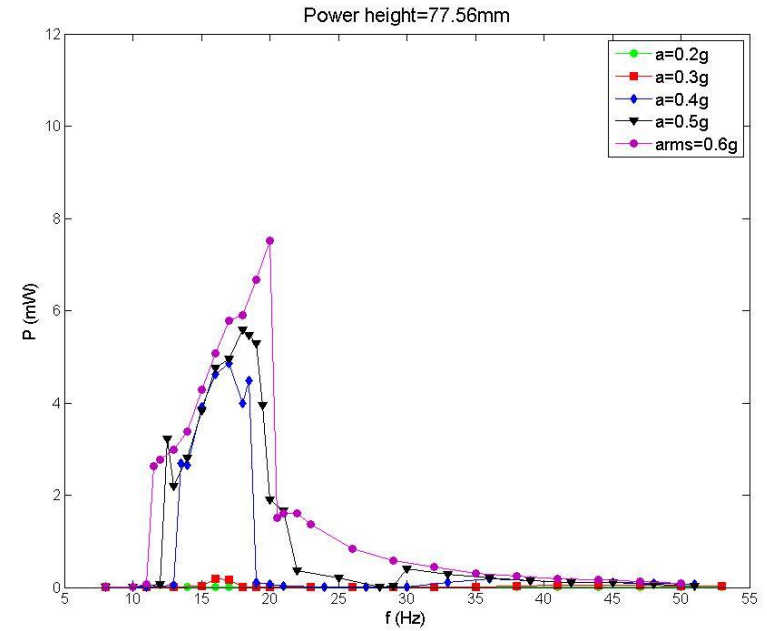
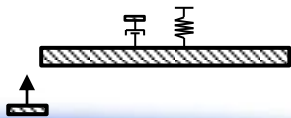
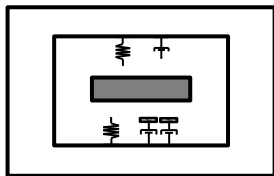
Cap height = 77.58 mm



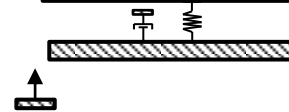
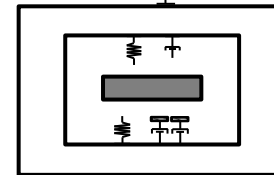
# Harvester Power Output



Cap height = 81.65 mm



Cap height = 77.58 mm



# Theoretical model

## 2 Dof system

Check the position of the mass:

- If it is connected to the lower spring

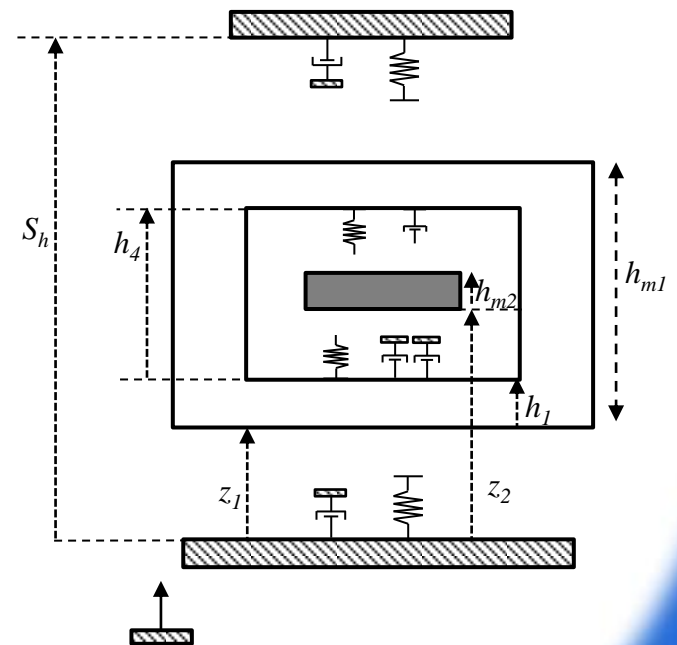
↓  
**oscillator equations**

- If it is not connected to the spring

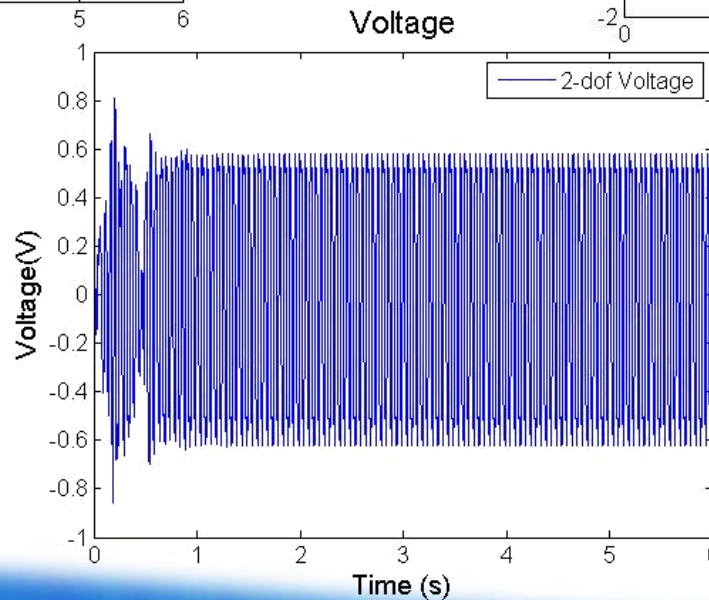
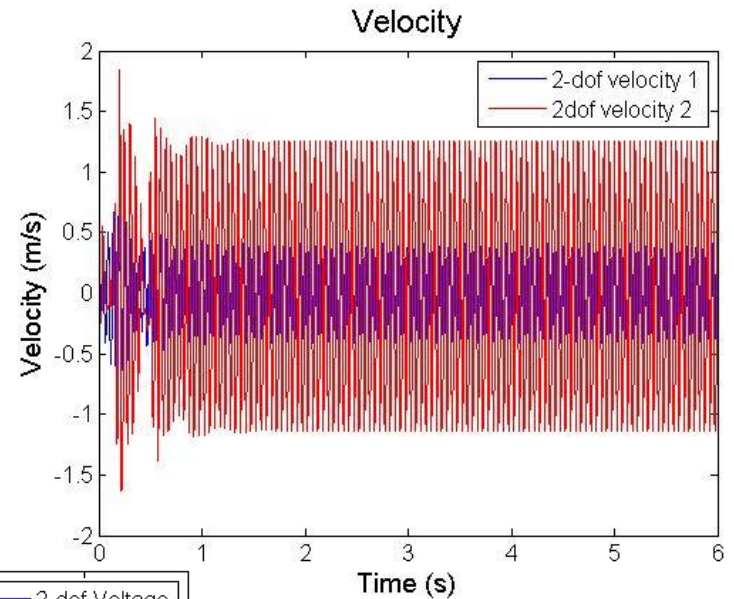
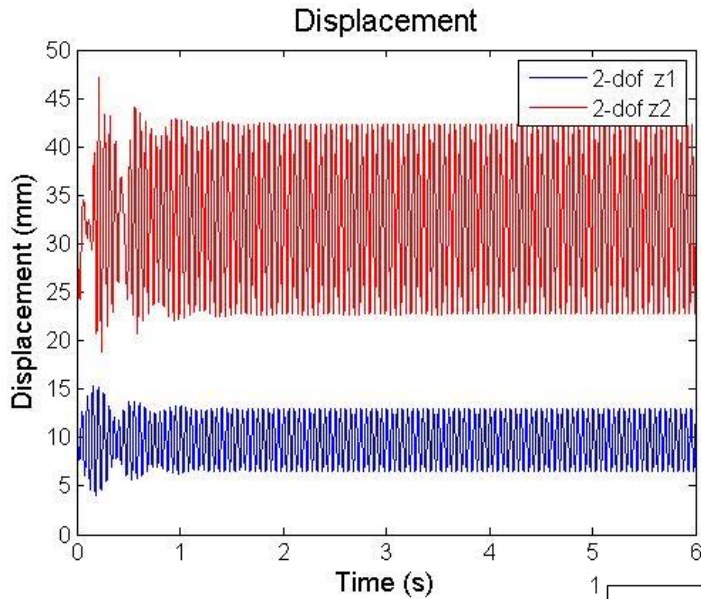
↓  
**free motion equations**

- If it connected to the spring on the top

↓  
**oscillator equations**



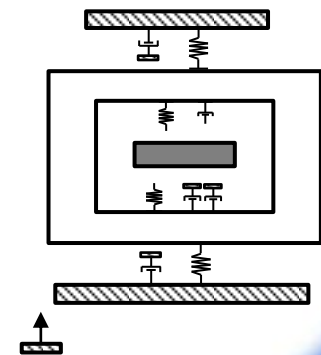
# Theoretical model



Cap Height = 77.56mm

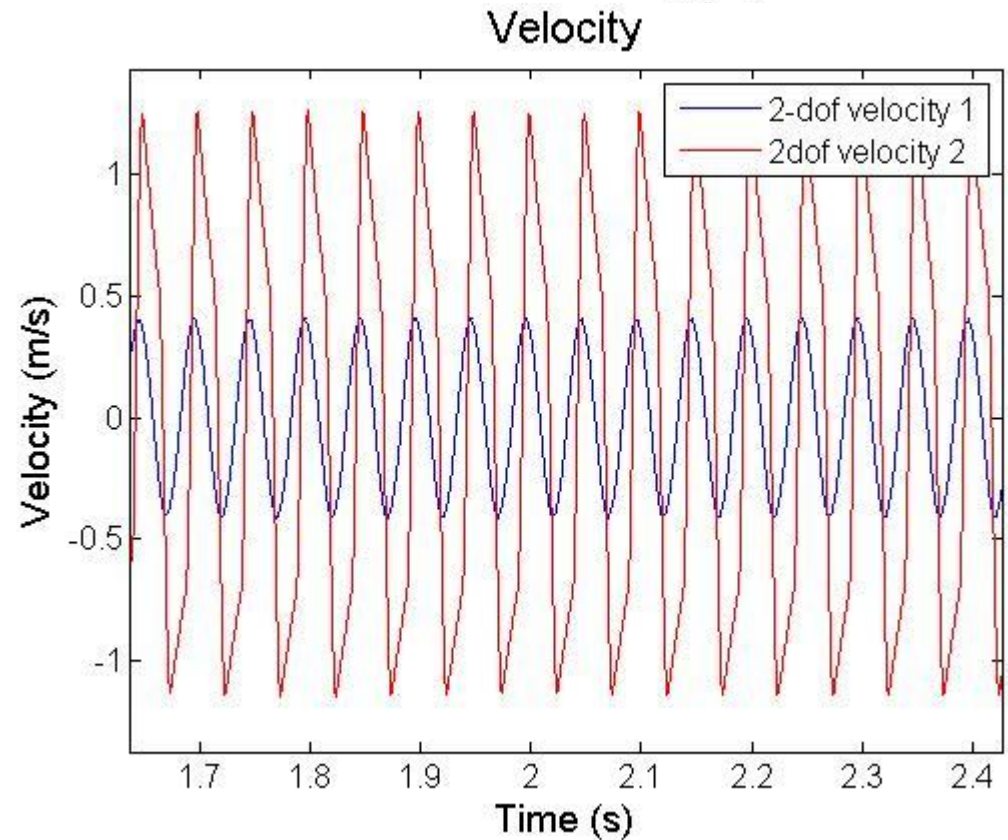
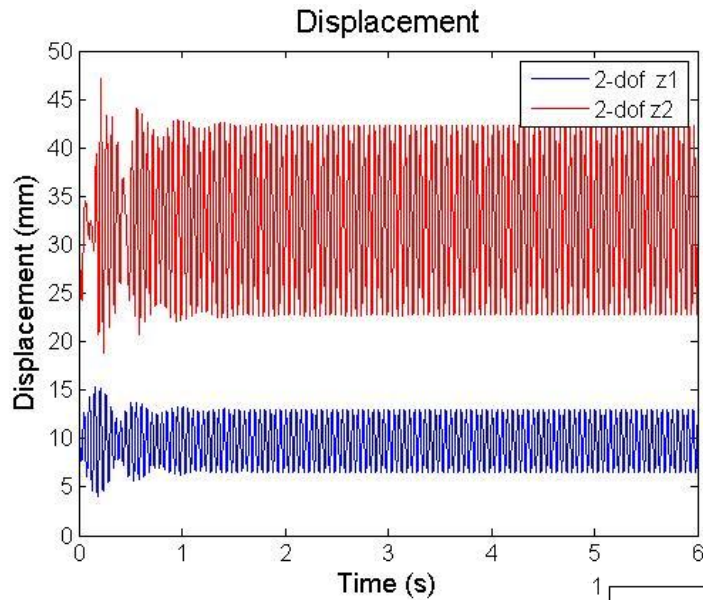
Excitation:

- Sine Wave
- $f=20\text{ Hz}$
- $a_{rms}=0.4\text{ g}$





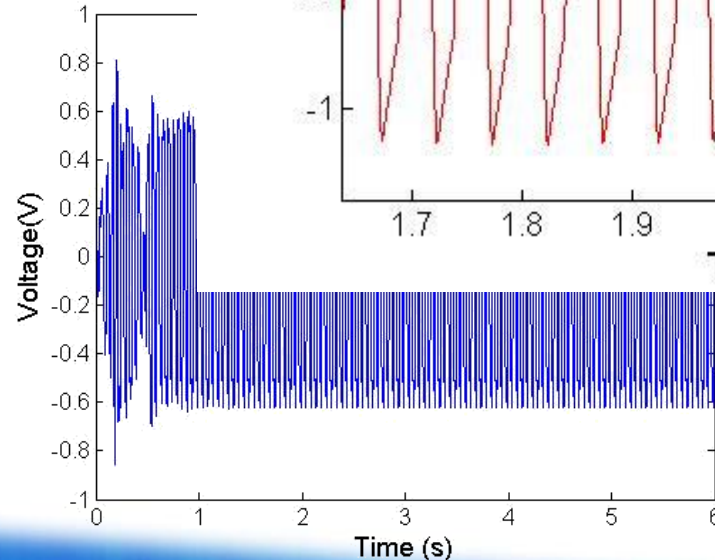
# Theoretical model



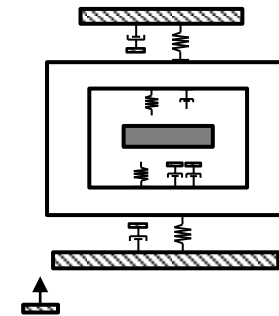
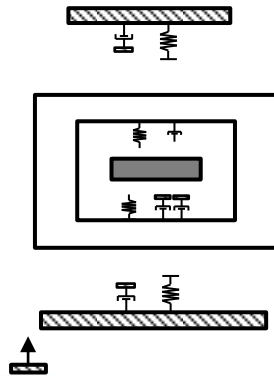
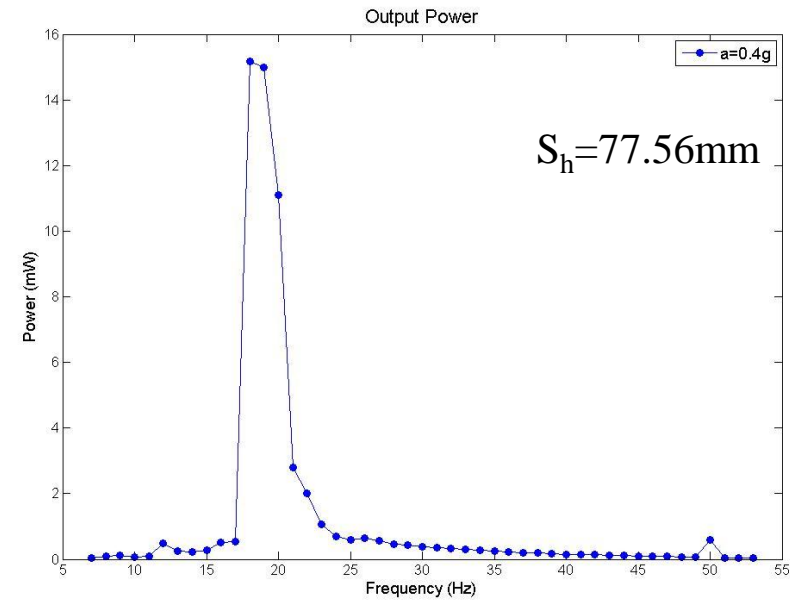
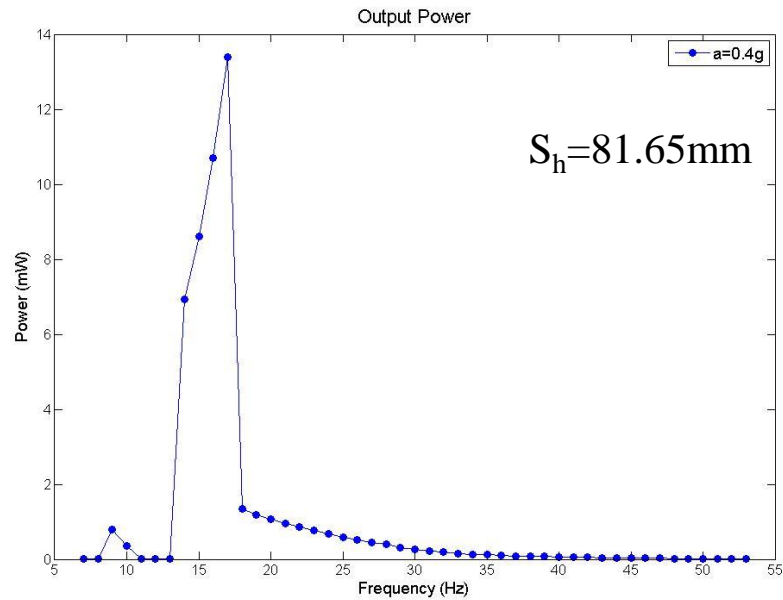
Cap Height = 77.56mm

Excitation:

- Sine Wave
- $f=20\text{ Hz}$
- $a_{rms}=0.4\text{ g}$



# Theoretical model



# Conclusion

- Description of a 2-Dof velocity amplified energy harvester
- Experimental results show two peaks at low acceleration amplitude and a wider response at higher acceleration.
- Theoretical model of a 2-Dof energy harvester
- Simulations show velocity amplification

## Future work

Miniaturization of the harvester

**THANKS  
FOR THE  
ATTENTION!**

