

# Nonlinear Energy Harvesting

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and Wisepower srl

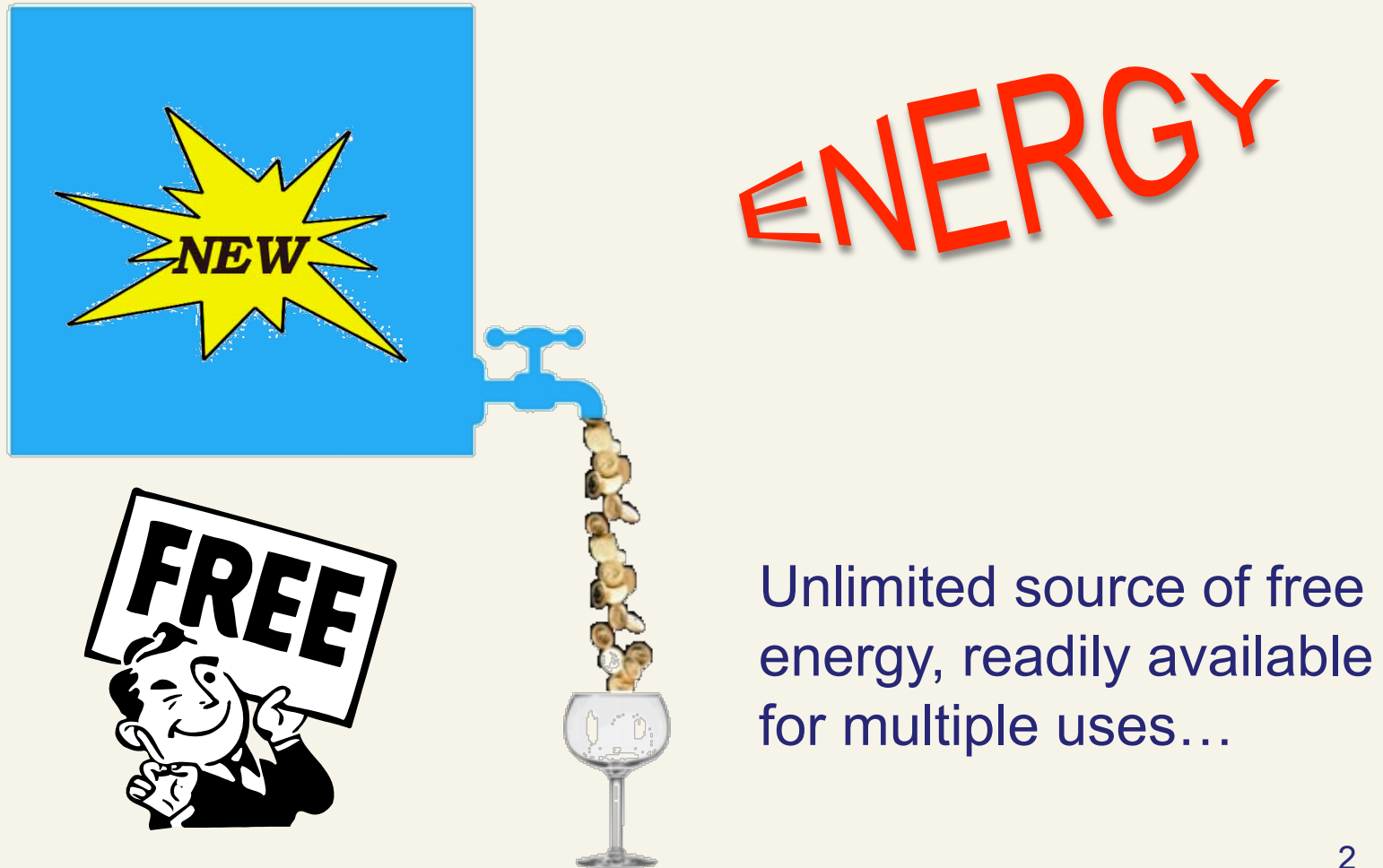
[www.nipslab.org](http://www.nipslab.org)

**N.i.P.S** Laboratory  
Noise in Physical Systems



ICAND2010 – Lake Louise, AL (CA) – 21-24 Sept. 2010

## Harvesting Energy....



Unlimited source of free energy, readily available for multiple uses...

Motivation: future ICT

There is an increasing demand of portable power

POWERING THE DIGITAL AND WIRELESS REVOLUTION

**PORTABLE POWER**

2005

September 18-21, 2005  
The Palace Hotel  
San Francisco

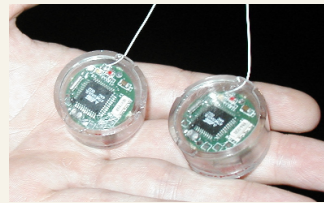
[www.PORTABLEPOWER2005.com](http://www.PORTABLEPOWER2005.com)

A must-attend event for portable device designers and OEMs!

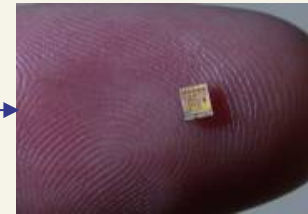
The poster features a blue header with the title 'POWERING THE DIGITAL AND WIRELESS REVOLUTION'. Below this, the main title 'PORTABLE POWER' is displayed in large, bold, orange letters, with '2005' in white on a green geometric shape. To the right of the title is a collage of images showing a hand holding a coin, a circuit board, a mobile phone, and a laptop. The event dates and location are listed below the title, followed by the website URL. At the bottom, a blue banner states 'A must-attend event for portable device designers and OEMs!'.

# Wireless sensor networks

- Small ( $<1\text{cm}^3$ )
- Lightweight ( $<100\text{ gr}$ )
- **Low Power ( $<100\text{ }\mu\text{W}$ )**
- Long-lasting (2-10 yr)
- Inexpensive ( $<1\text{ \$}$ )
- Low data rate
- wireless platforms
- Flexibility



Present  
(cubic centimeter)



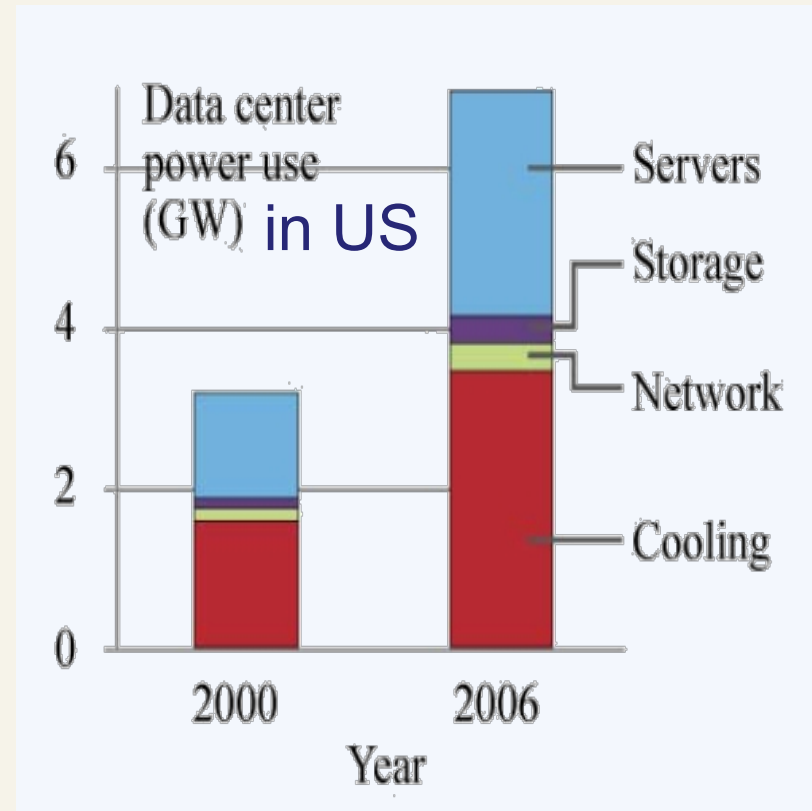
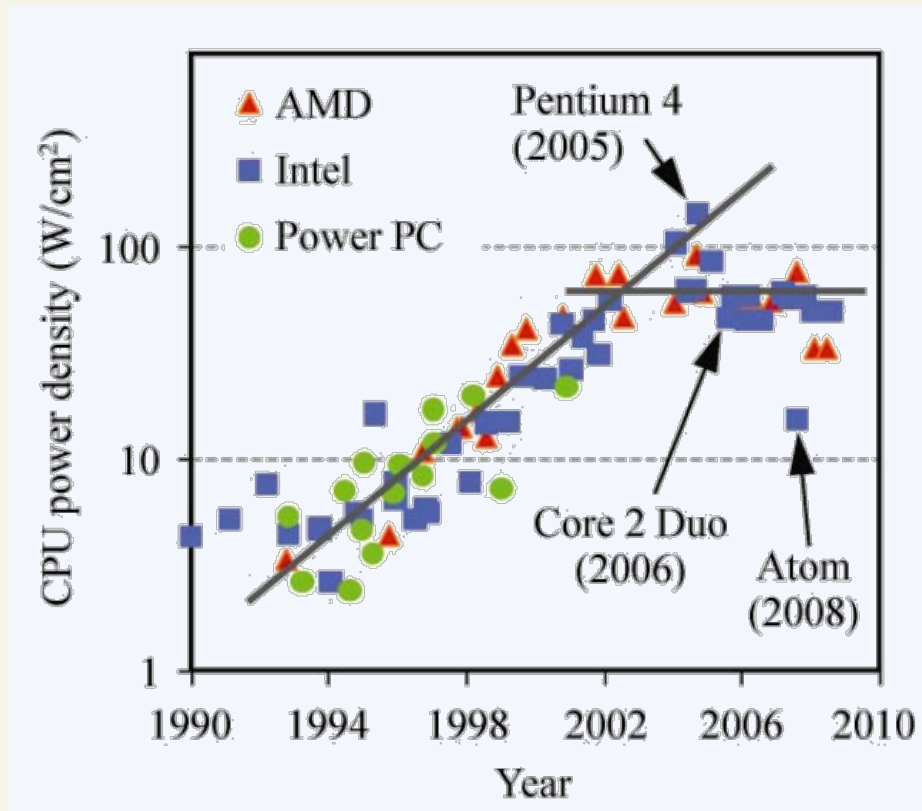
Future  
(cubic sub-millimeter  
sub-micrometer)



Monitoring and controlling different environments through a **network of small, distributed, cheap, low consumption, adaptable, interconnected, smart devices** represents a new important opportunity that is rapidly becoming a reality.

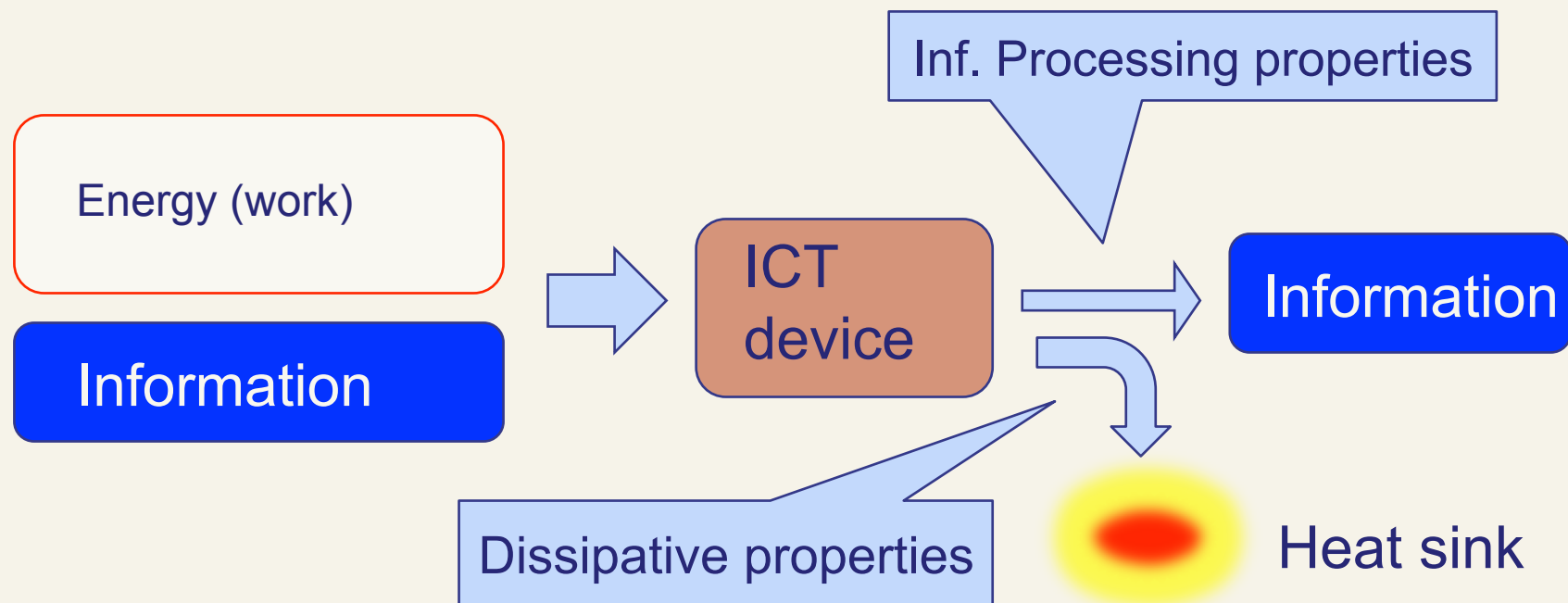
# ICT, dissipation, fluctuation

Quite recently ICT (Information and Communication technology) has become an interesting playground for fluctuations due to the presence of significant **dissipation**...



# Let's give a closer look at the problem

An **ICT device** is a machine that inputs **information** and **energy** (under the form of work), processes both and outputs information and energy (mostly under the form of heat).



**Energy efficiency** is usually defined as the percentage of energy input to a device that is consumed in useful work and not wasted as useless heat

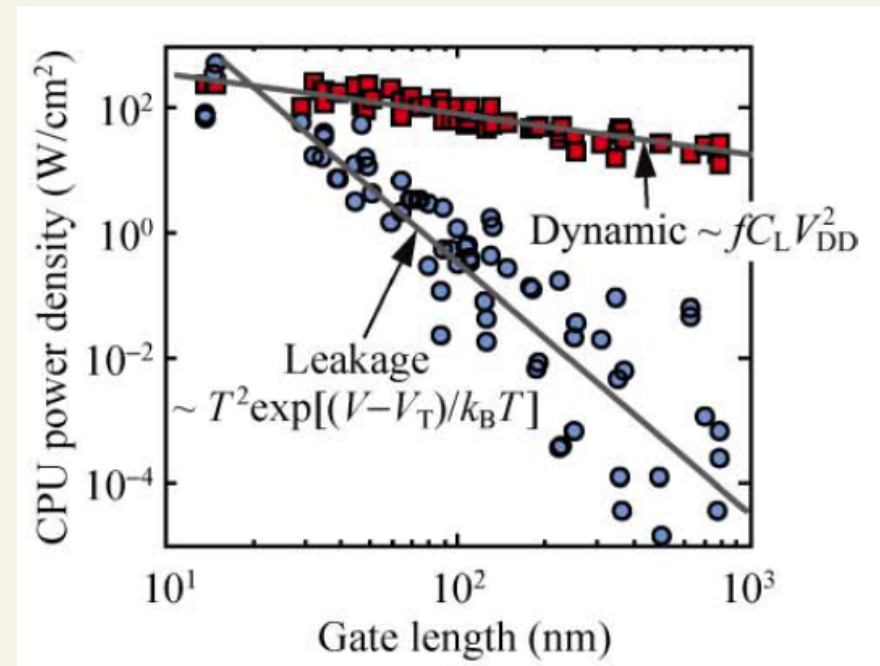
# The energy efficiency issue: some clues...

Three components have been identified for digital power consumption:

- **dynamic** power used during switching (for charging and discharging the inverter load)
- subthreshold **leakage** power
- short-circuit power

However the present modelling of energy dissipation mechanism is based on microscale 3D system templates and is NOT adequate to represent nanoscale 3D, 1D devices...

Knowledge needed



E. Pop, *Energy Dissipation and Transport in Nanoscale Devices*, Nano Res (2010) 3: 147

# The energy efficiency issue: some more clues...

There are fundamental physics **LIMITS** that are relevant

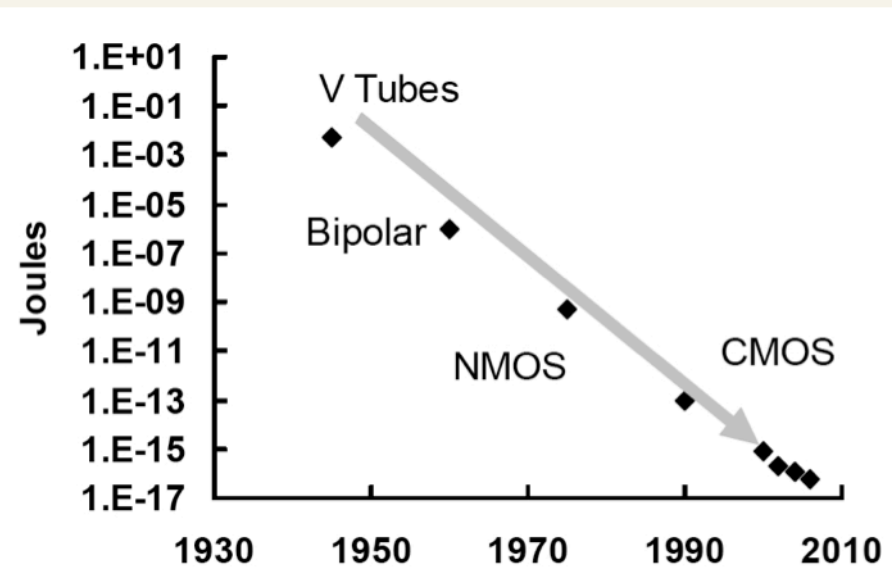
- 1 Landauer limit to minimum energy for logically irreversible operation

$$E_{\min} = KT \log 2 = 10^{-21} \text{ J}$$

- 2 Quantum limit from Energy/time uncertainty relation

$$\Delta t = \pi \hbar / 2E$$

Margolus, N. & Levitin, L. B.  
The maximum speed of dynamical evolution.  
Physica D 120, 188–195 (1998)



Energy per elementary logic operation. From: Shekhar Borkar, Electronics beyond nano-scale CMOS, Proceedings of the 43rd annual Design Automation Conference, p. 807, San Francisco, CA, USA, 2006



# The energy efficiency issue: some more clues...

There are fundamental physics **ISSUES** that are relevant

- 1 Nanoscale thermodynamics **vs** macroscale thermodynamics  
Hill, Terrell, L., (2001). "Nanothermodynamics", *Nanoletters*, 1, 111, 273
- 2 Non-equilibrium statistical mechanics **vs** standard statistical mechanics
- 3 Linear dynamics **vs** Nonlinear dynamics

At the nanoscale, in fact, thermal fluctuations, negligible at higher scale, become the most relevant factor and non-equilibrium thermodynamics approaches are required as opposed to the traditional concepts based on equilibrium energy balances. *Non-equilibrium work relations*, mainly in the form of "fluctuation theorems", have shown to provide valuable information on the role of *non-equilibrium* fluctuations.

- Bustamante, C., Liphardt, J. and Ritort, F., *The nonequilibrium thermodynamics of small systems*, PHYSICS TODAY, 2005, 58, p.43-48.
- F. Ritort, *Work fluctuations, transient violations of the second law and free-energy recovery methods: Perspectives in Theory and Experiments*, Poincare Sem. 2 (2003) 193.
- Gallavotti G., Cohen E.G.D., *Dynamical ensembles in nonequilibrium statistical mechanics*, Phys Rev Lett, 2694 (1995).
- Rubi, J Miguel, "Does Nature Break the Second Law of Thermodynamics?"; Scientific American, October 2008

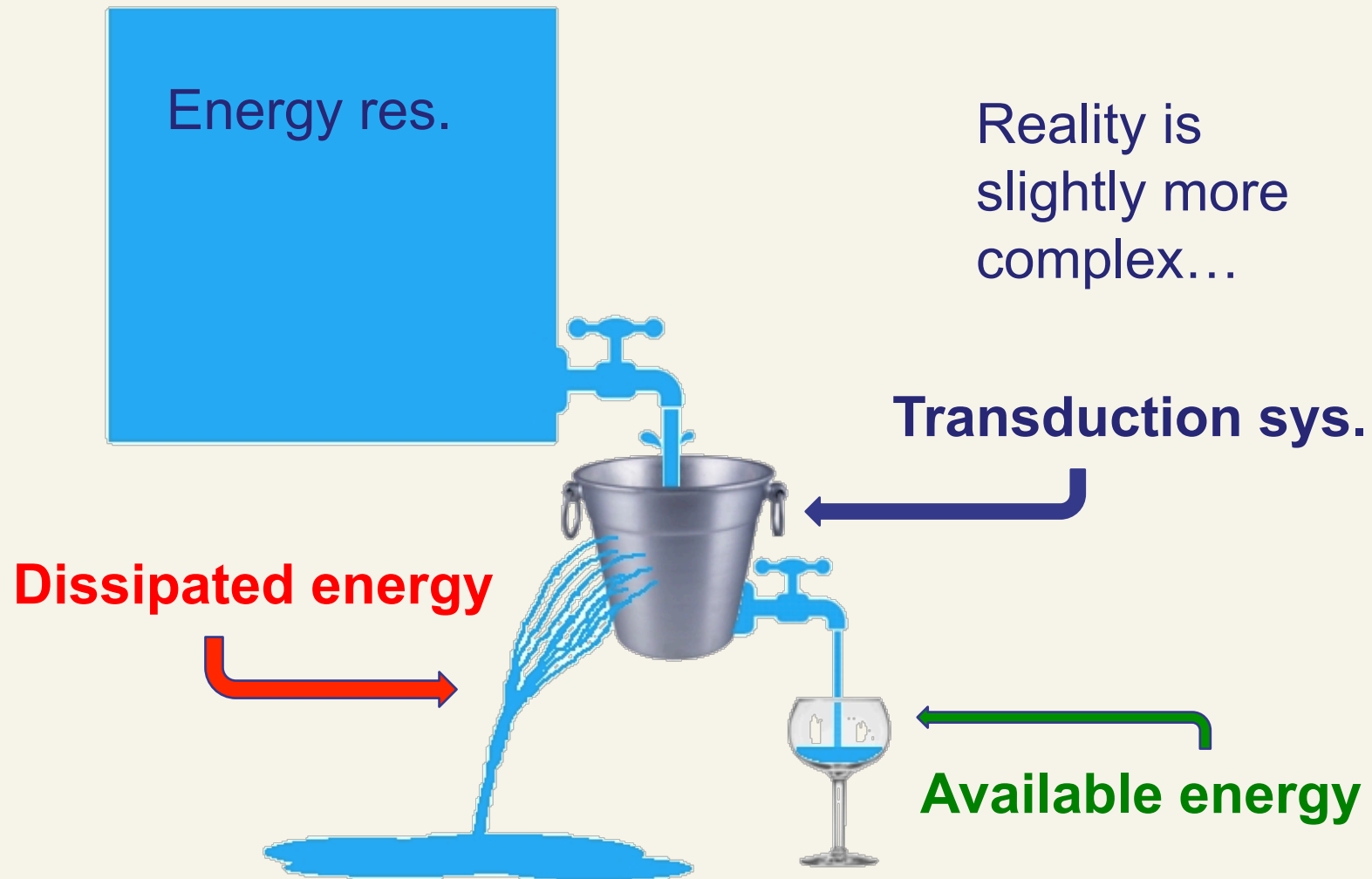
## Energy harvesting basic ideas...



# ENERGY

Unlimited source of free energy, readily available for multiple uses...

it is more like...



# Energy harvesting basic ideas

## Kinetic energy

wind

sound

Falling bodies

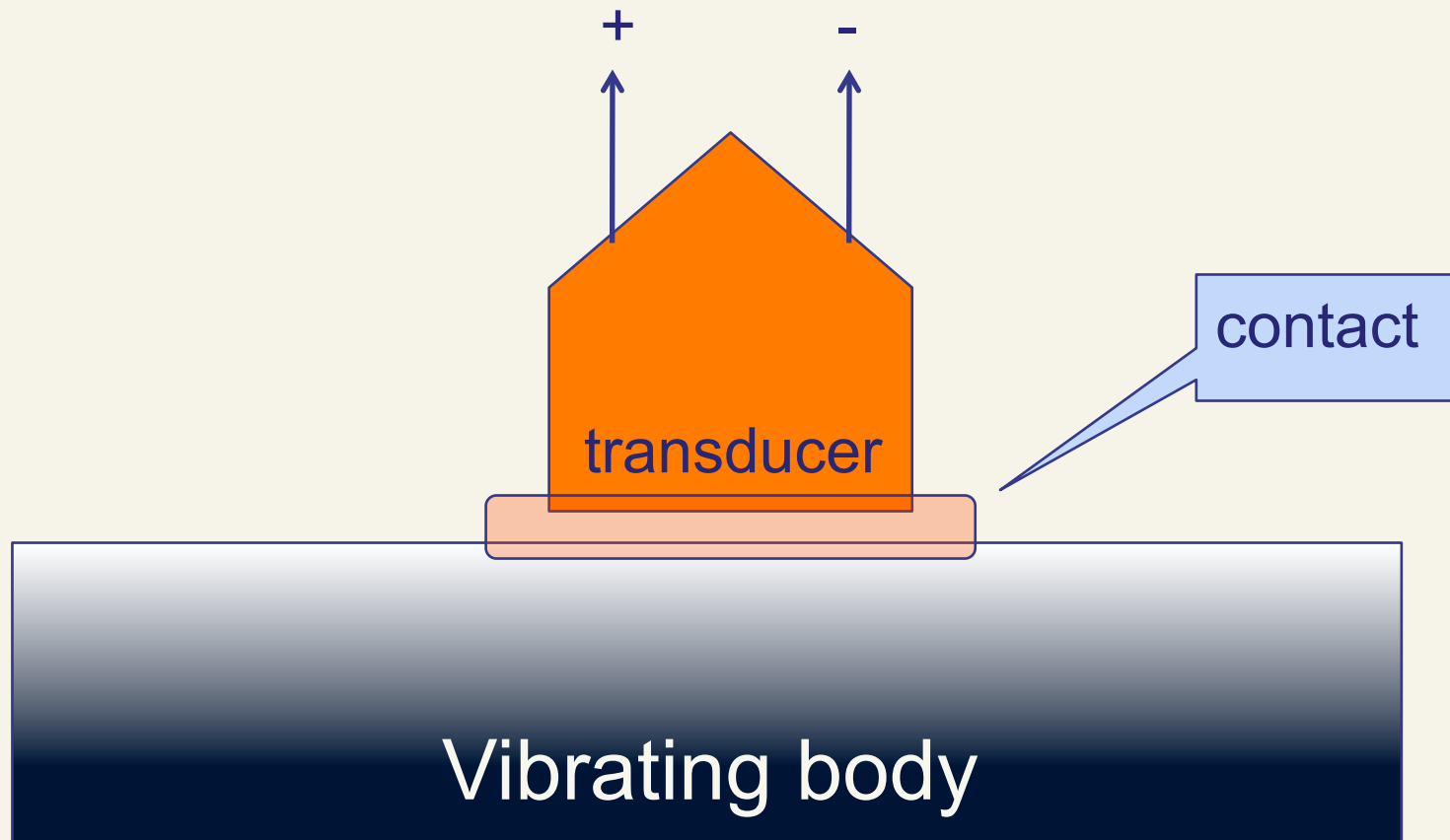
vibrations

water waves and tides

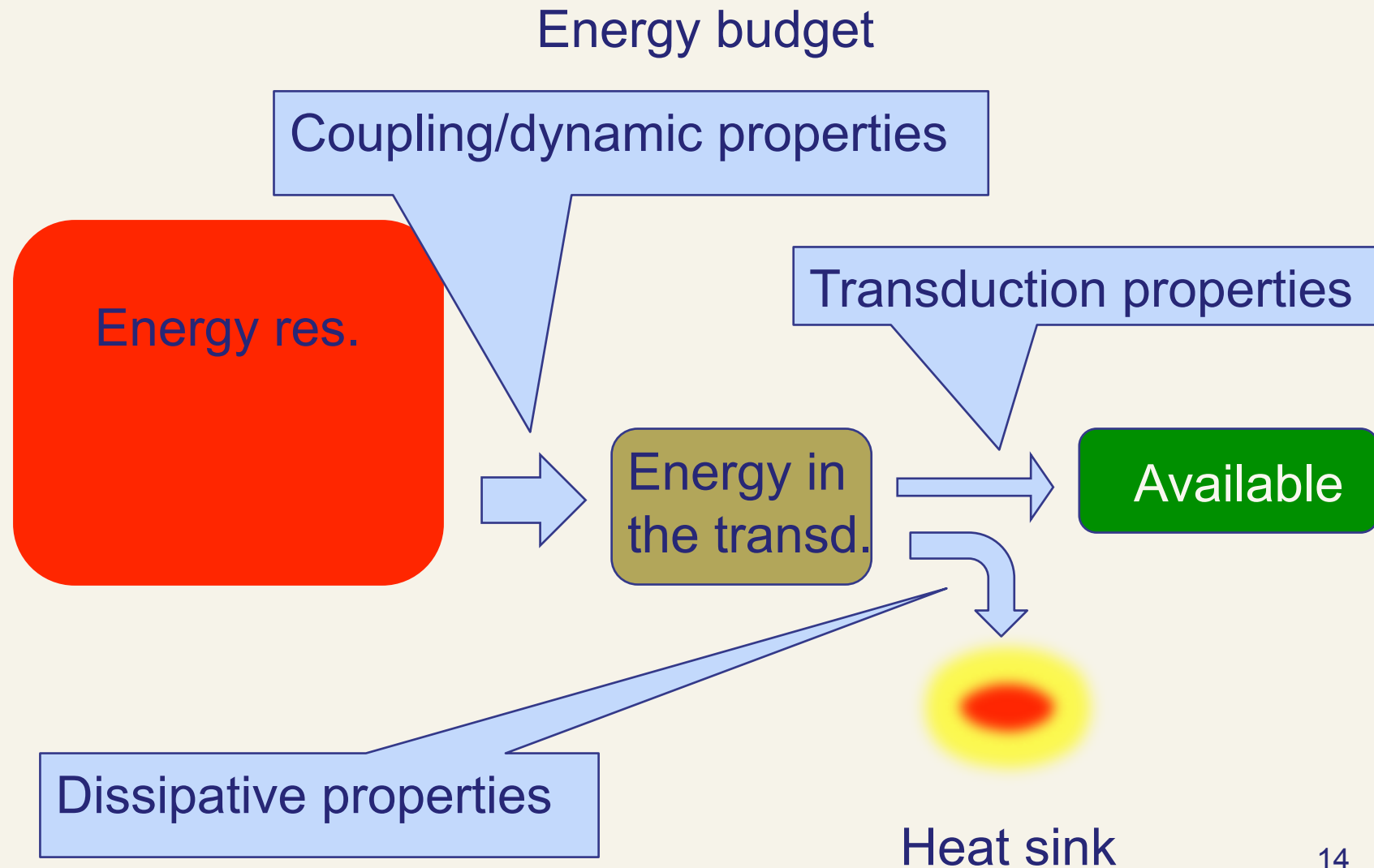
Focus on vibrations of solid bodies....

# Vibrations energy harvesting

## Basic Scheme

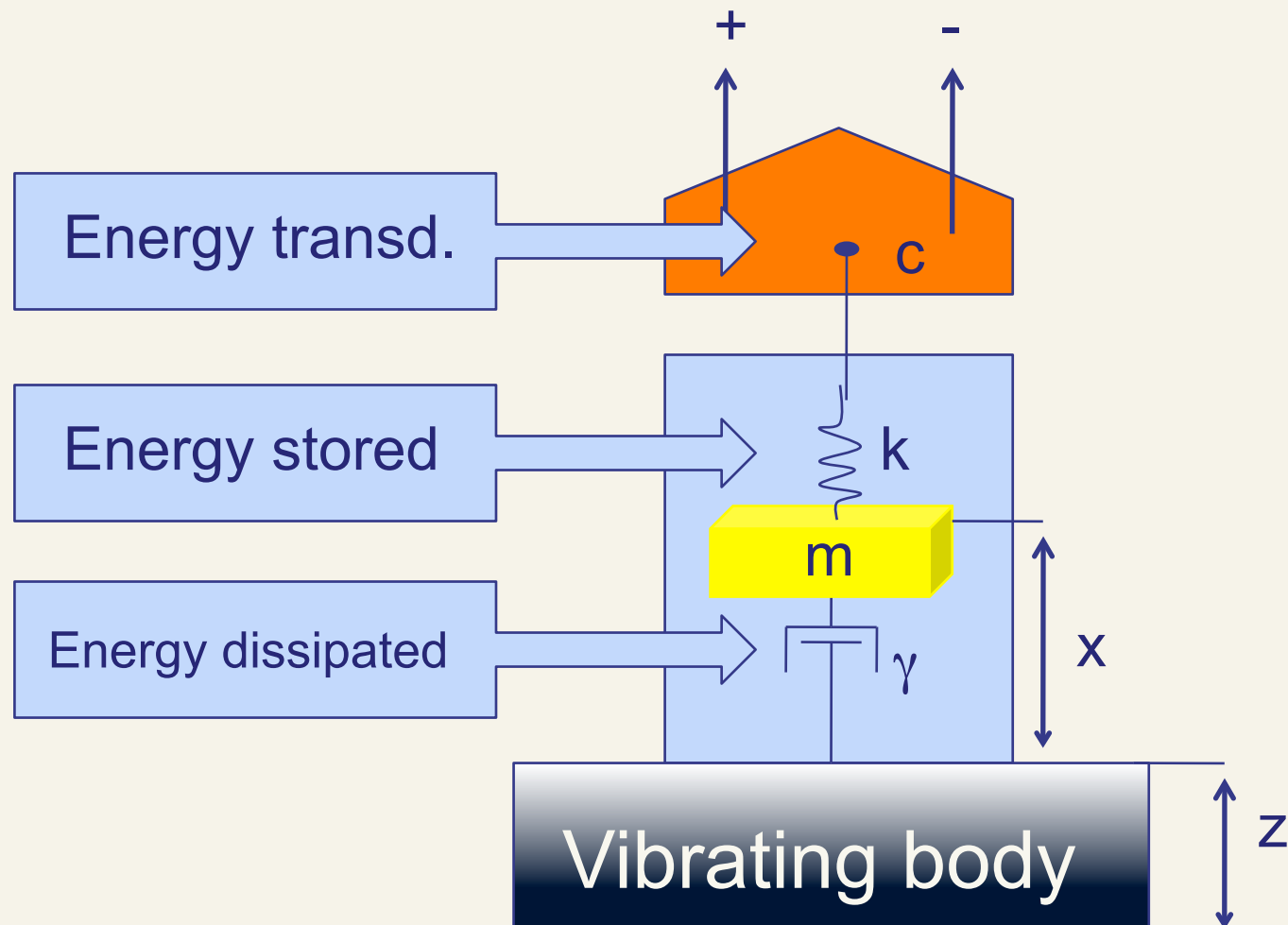


# Vibrations energy harvesting

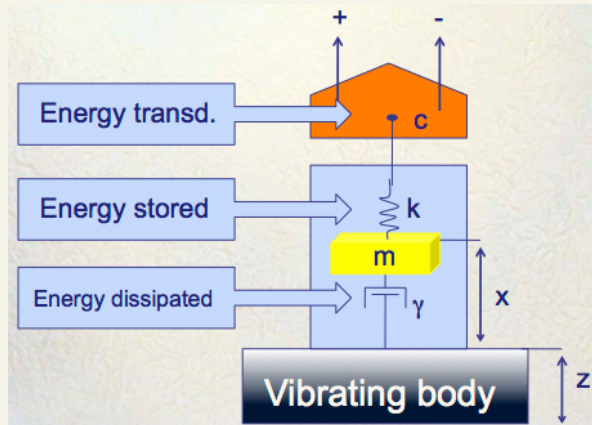


# Vibrations energy harvesting

## Dynamical model



# Vibrations energy harvesting



Dynamical model

$$m\ddot{x} = -\frac{dU(x)}{dx} - \gamma\dot{x} - c(x,V) + \xi_z$$

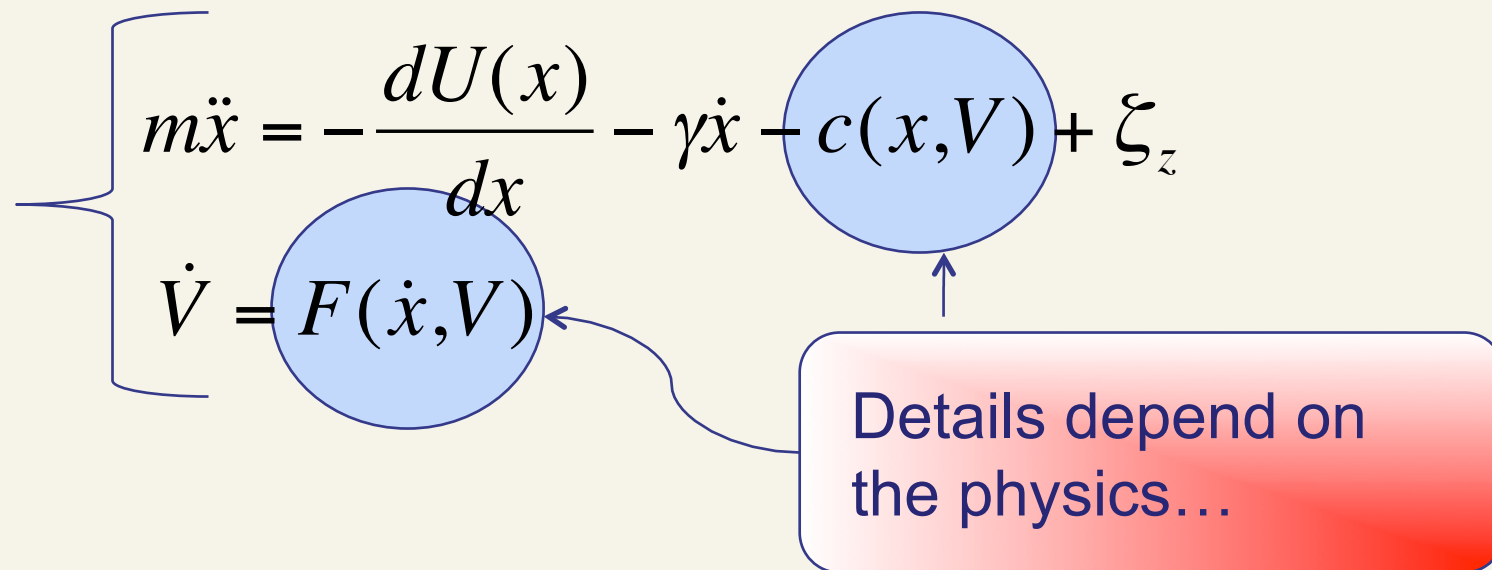
Where:  $U(x)$  Represents the Energy stored  
 $\gamma\dot{x}$  Accounts for the Energy dissipated  
 $c(x,V)$  Accounts for the Energy transduced  
 $\xi_z$  Accounts for the input Energy



# Vibrations energy harvesting

## Dynamical model

Equations that link the vibration-induced displacement with the Voltage


$$\left\{ \begin{array}{l} m\ddot{x} = -\frac{dU(x)}{dx} - \gamma\dot{x} - c(x,V) + \xi_z \\ \dot{V} = F(\dot{x}, V) \end{array} \right.$$

Details depend on the physics...

Three main transduction mechanisms...

# Vibrations energy harvesting

## Transduction mechanisms

1

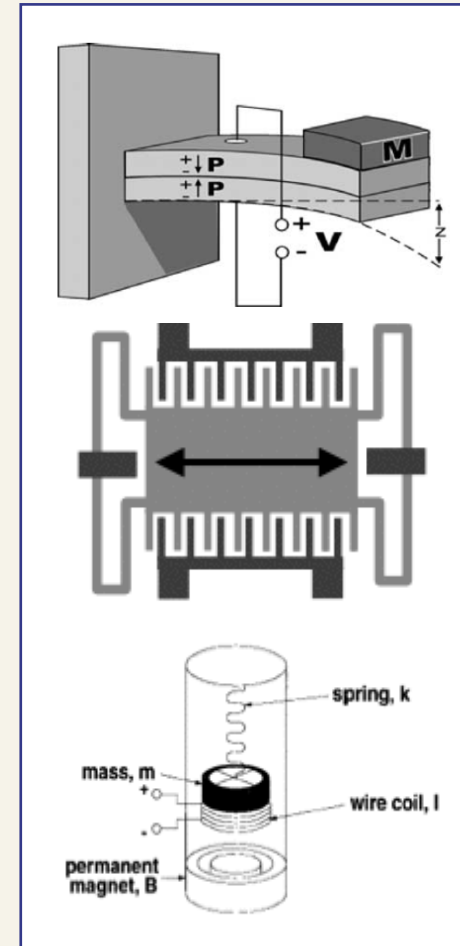
Piezoelectric: dynamical strain is converted into voltage difference.

2

Capacitive: geometrical variations induce voltage difference

3

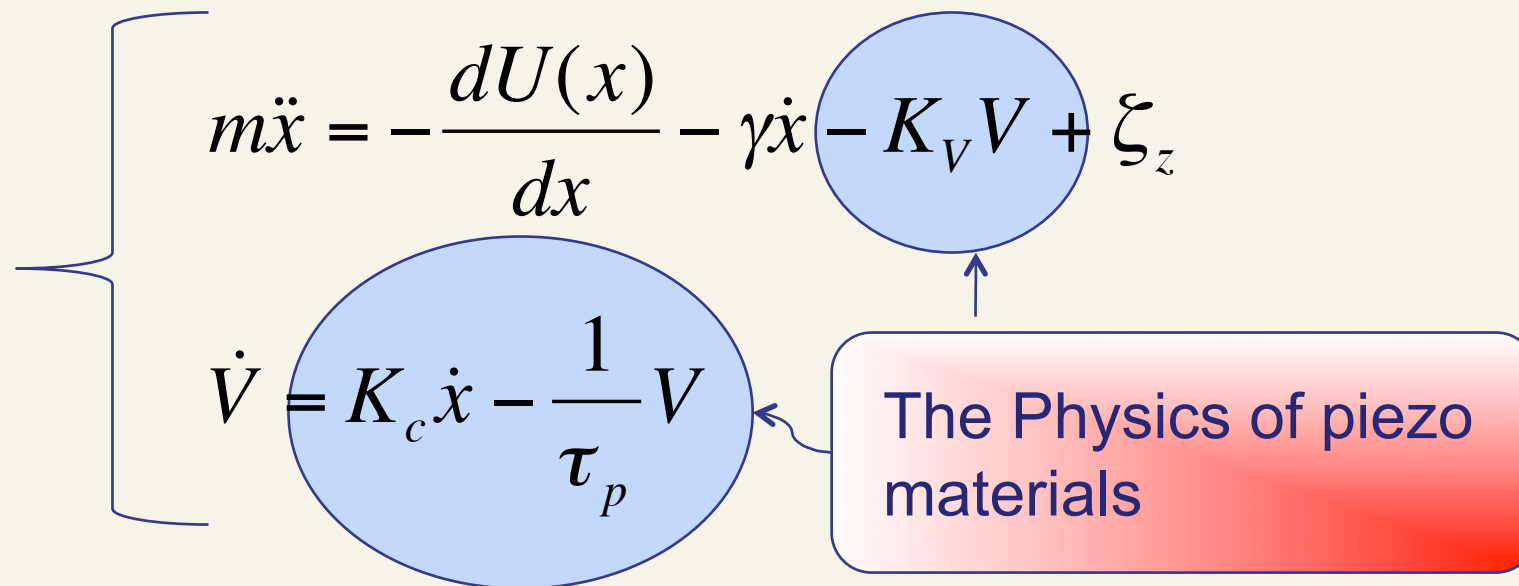
Inductive: dynamical oscillations of magnets induce electric current in coils



# Vibrations energy harvesting

## Transduction mechanisms

- 1 Piezoelectric: dynamical strain is converted into voltage difference.



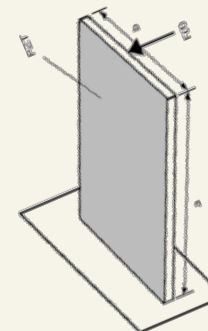
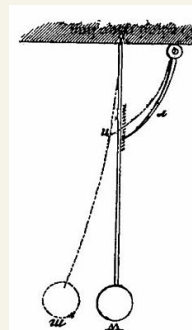
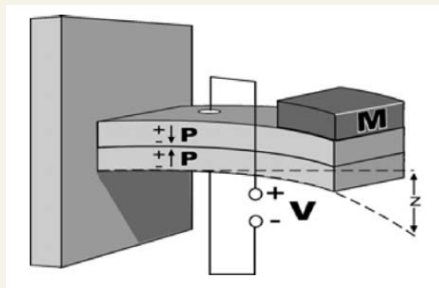
The available power is proportional to  $V^2$

## Linear systems

When  $U(x) = \frac{1}{2}kx^2$  it is called a linear system

Linear systems have some interesting features... (and engineers like them most)

- 1) There exist a simple math theory to solve the eq.s
- 2) They have a resonant behaviour (resonance freq.)
- 3) They can be “easily” realized with catilevers and pendula



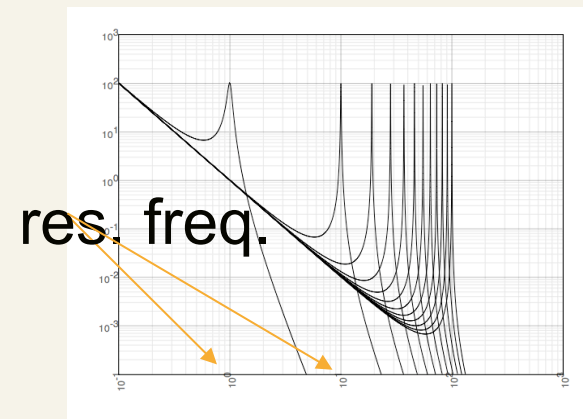
# Vibrations energy harvesting

## Linear systems

For a linear system the transfer function presents one or more peaks corresponding to the resonance frequencies and thus it is efficient mainly when the incoming energy is abundant in that regions...

This is a serious limitation when you want to build a small energy harvesting system...

Why ?!!



# Vibrations energy harvesting

## Linear systems

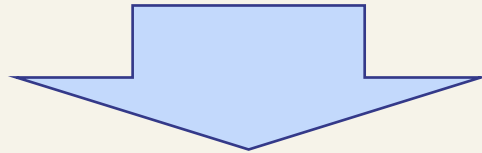
For two main reasons...

- (1) the frequency spectrum of available vibrations instead of being sharply peaked at some frequency is usually very broad.
- (2) The frequency spectrum of available vibrations is particularly rich in energy in the low frequency part... and it is very difficult, if not impossible, to build small low-frequency resonant systems...

# Vibrations energy harvesting

Whish list for the perfect vibration harvester

- 1) Capable of harvesting energy on a broad-band
- 2) No need for frequency tuning
- 3) Capable of harvesting energy at low frequency

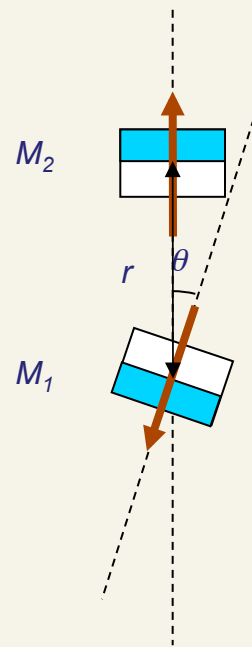
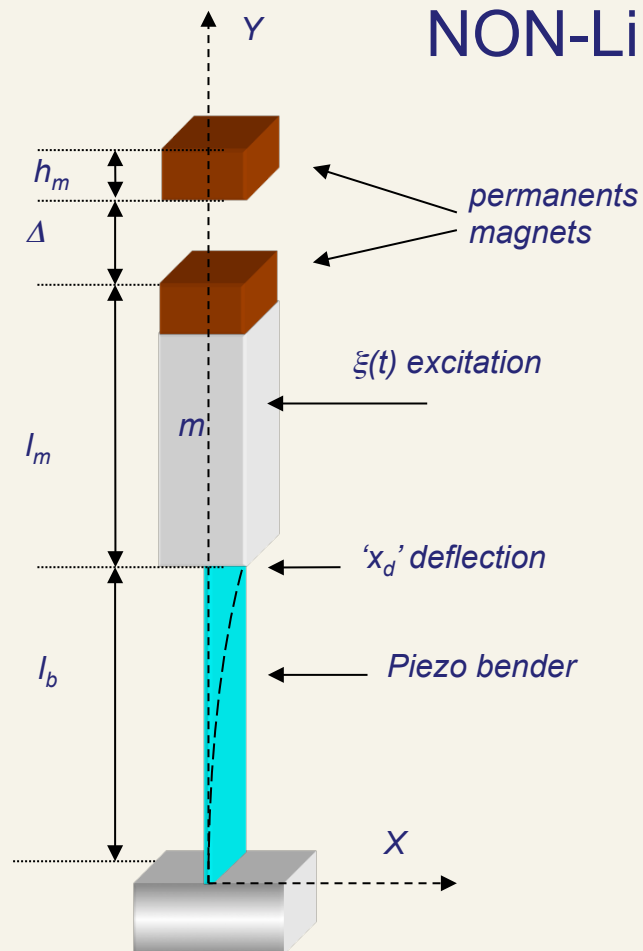


- 1) Non-resonant system
- 2) “Transfer function” with wide frequency resp.
- 3) Low frequency operated

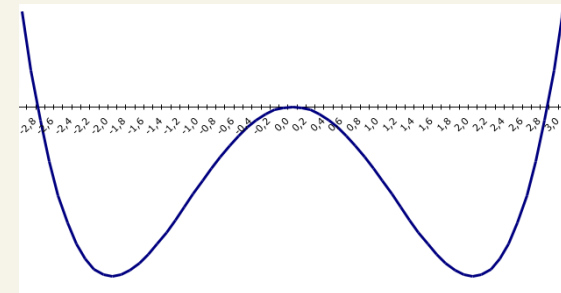
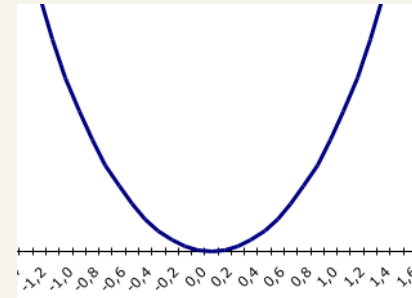
# Vibrations energy harvesting

## NON-Linear mechanical oscillators

### NON-Linear Inverted pendulum

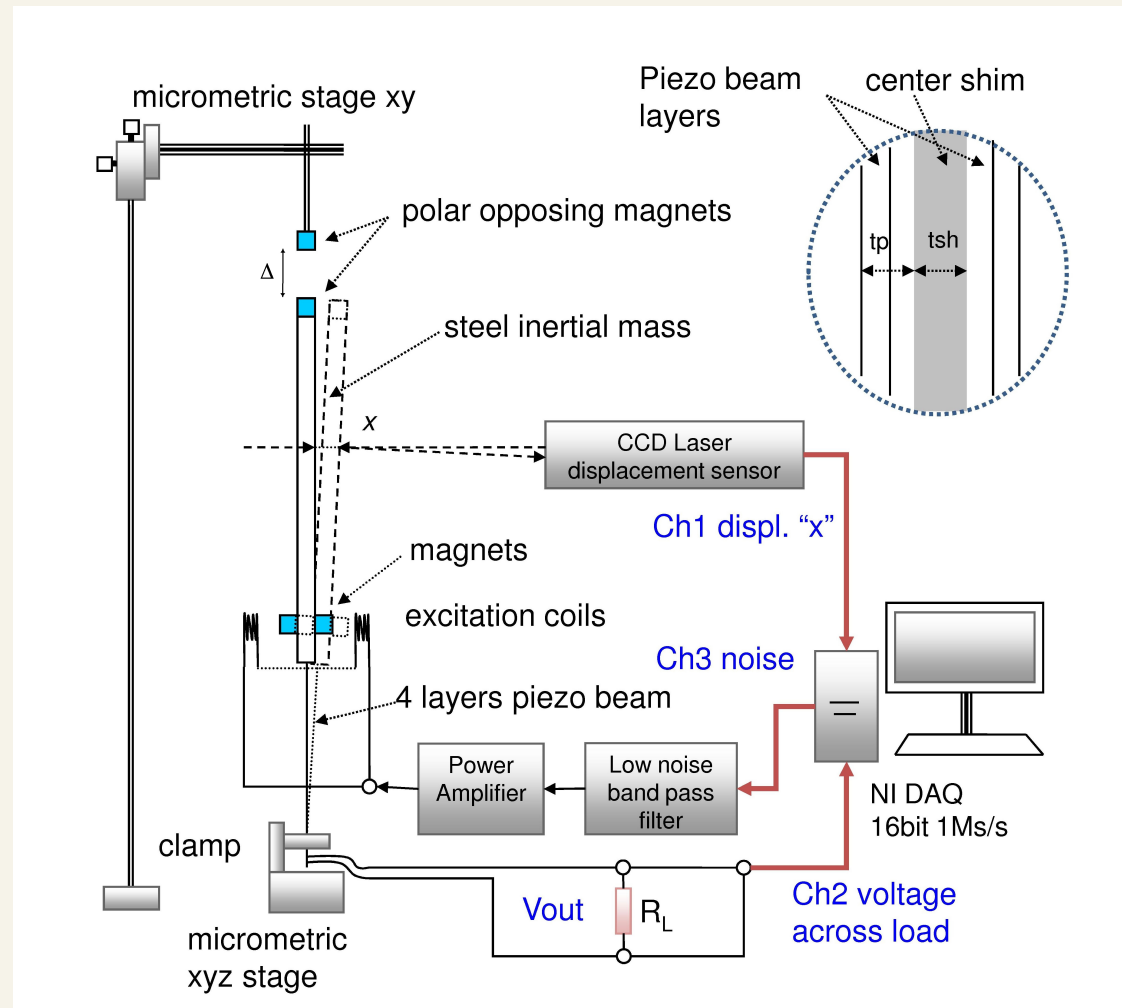


b)



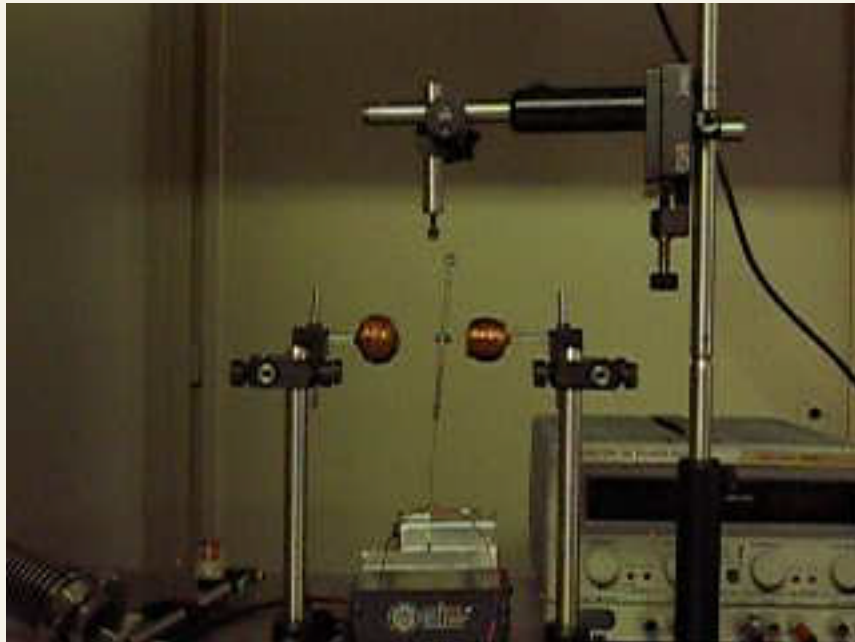


## NON-Linear mechanical oscillators

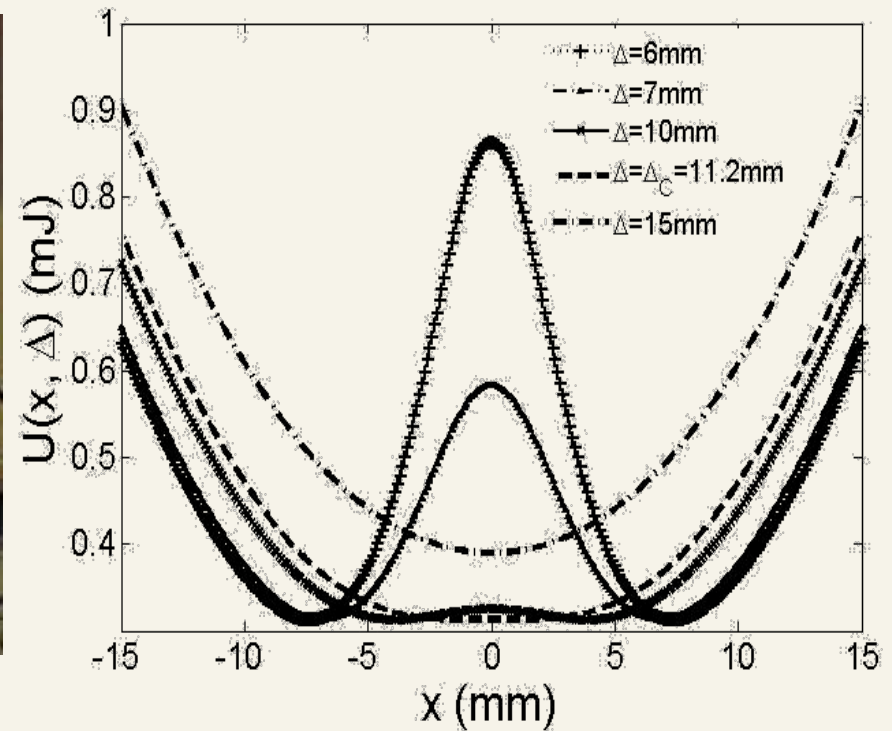


# Vibrations energy harvesting

## NON-Linear mechanical oscillators

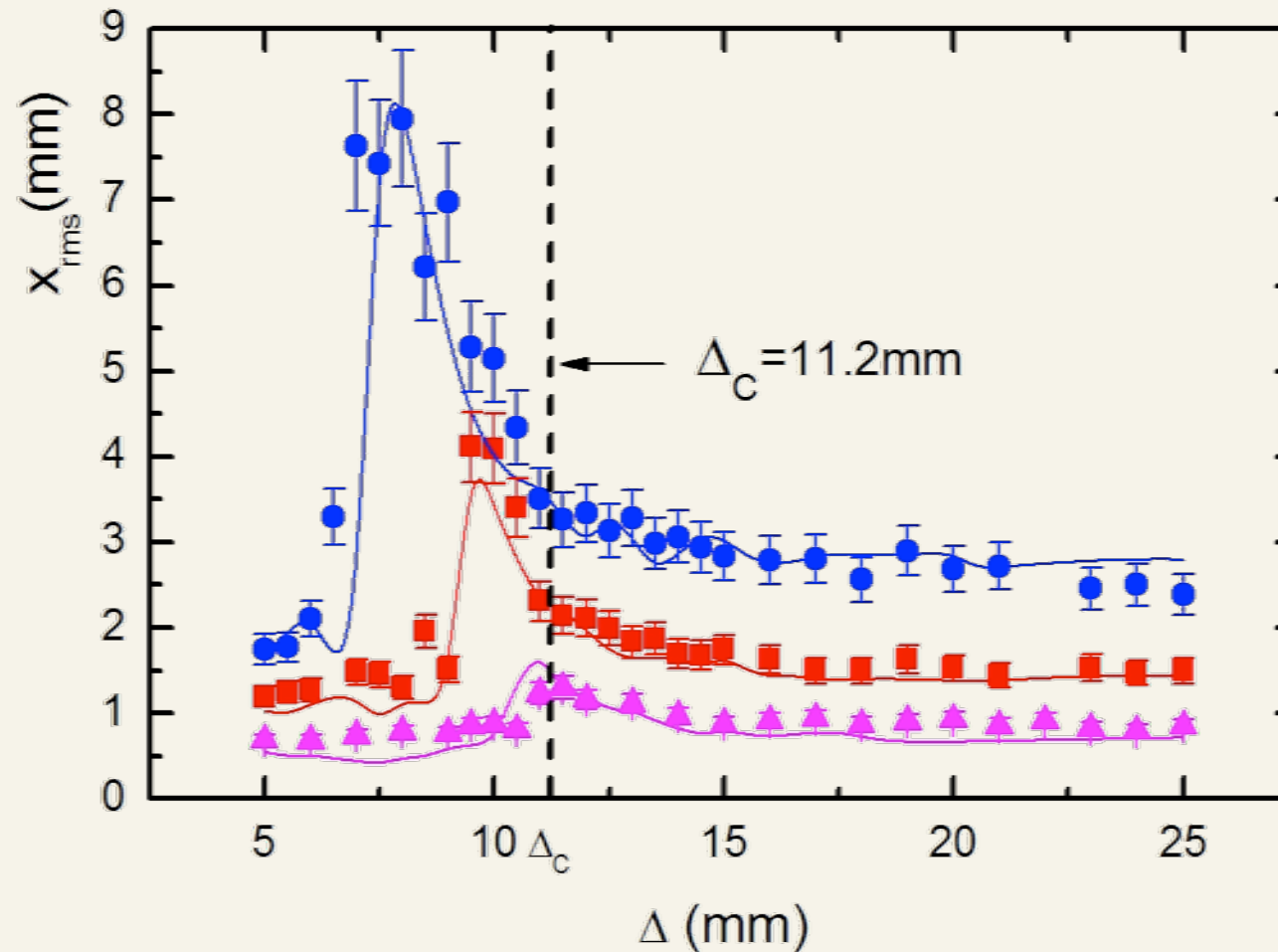


<http://www.nipslab.org/node/1676>



# Vibrations energy harvesting

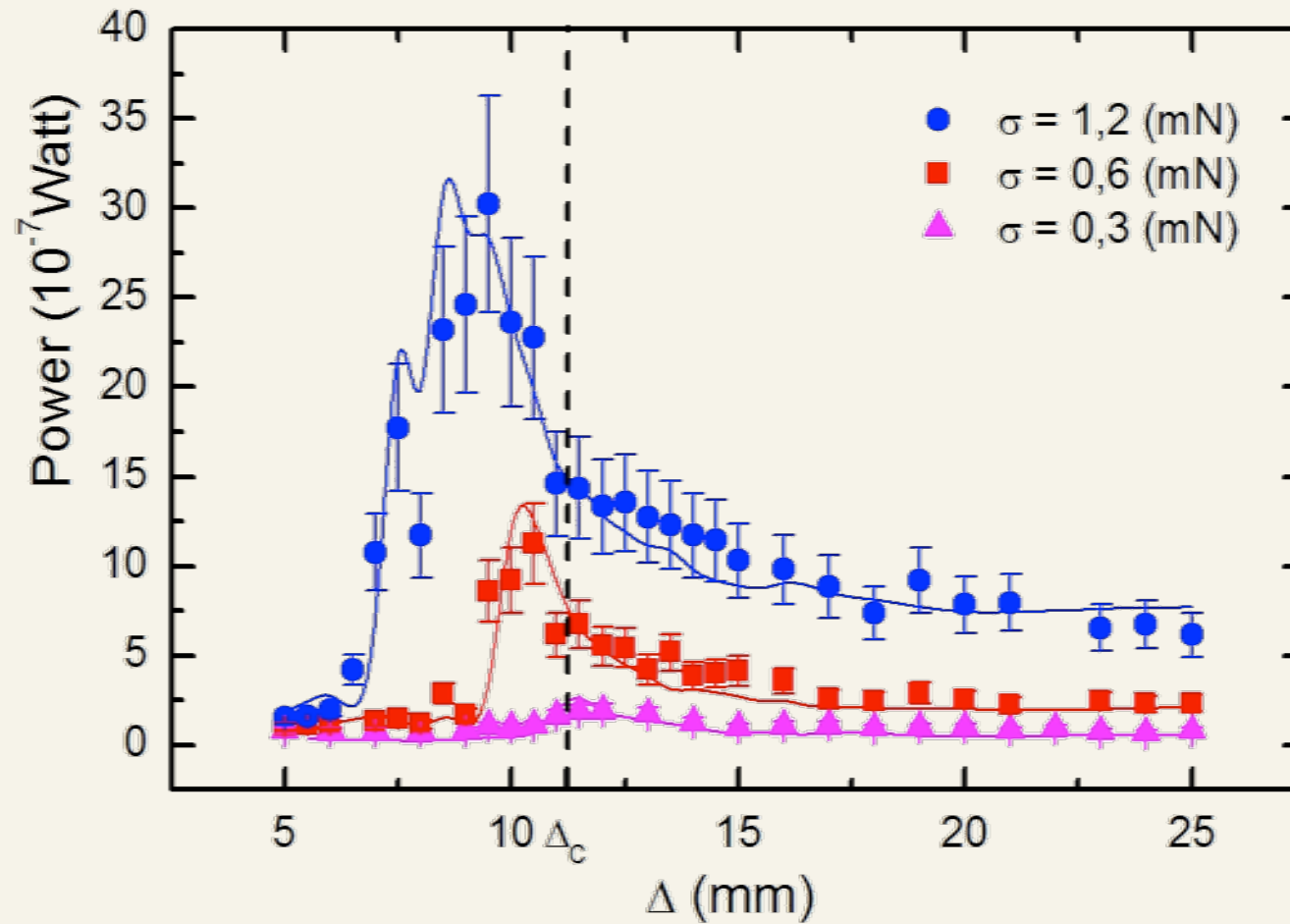
## NON-Linear mechanical oscillators



Nonlinear Energy Harvesting, F. Cottone; H. Vocca; L. Gammaitoni , Physical Review Letters, 102, 080601 (2009)

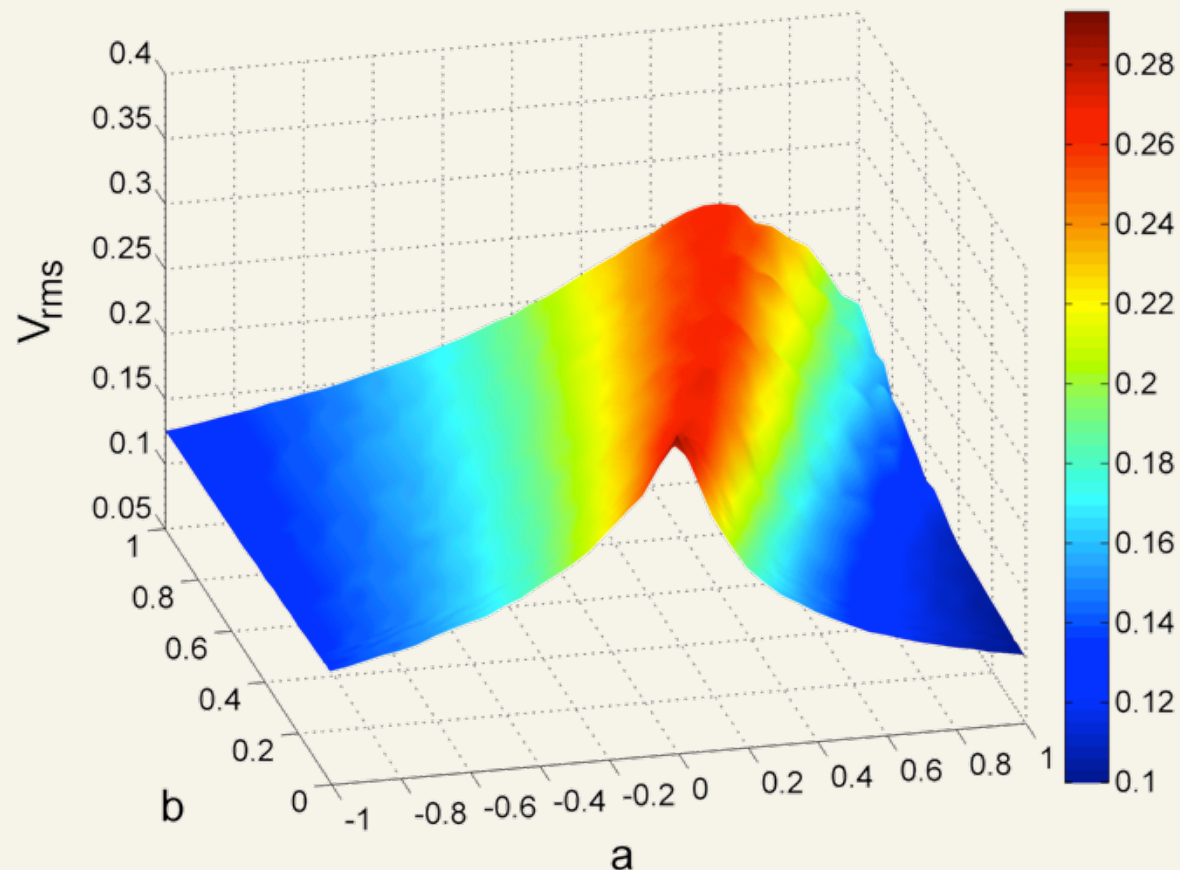
# Vibrations energy harvesting

## NON-Linear mechanical oscillators



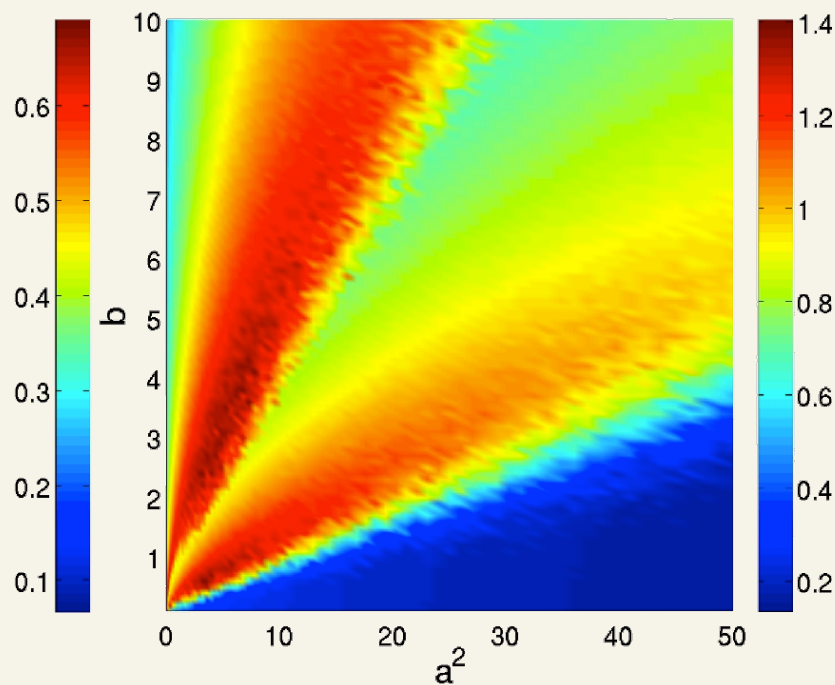
# Noise energy harvesting

$$U(x) = -\frac{1}{2}ax^2 + \frac{1}{4}ax^4 \quad \text{Duffing potential}$$



# Noise energy harvesting

$$U(x) = -\frac{1}{2}ax^2 + \frac{1}{4}ax^4 \quad \text{Duffing potential}$$



$$b_{MAX} = \frac{a^2}{4D \log(\tau_p)}$$

## To think about...

- 1) Non resonant (i.e. non-linear) mechanical oscillators can outperform resonant (i.e. linear) ones\*
- 2) Non-linear systems are more difficult to treat
- 3) Bistability is not the only nonlinearity available... see:  
L. Gammaitoni, I. Neri, H. Vocca, Appl. Phys. Lett. 94, 164102 (2009)

\* **wisepower technology**, patent pending. For more info see: [www.nipslab.org](http://www.nipslab.org), [www.wisepower.it](http://www.wisepower.it)

# ICT related initiatives funded by EC



6 partners: Wurzburg (Ger), ICN (Sp), VTT (Fi), Univ Geneva (Ch), Unicam (It)  
2.6 M€, 3 years, lead by NiPS  
[www.nanopwr.eu](http://www.nanopwr.eu)



4 partners: UAC (Sp), Tyndal (Ir), Univ Glasgow (UK)  
0.6 M€, 3 years, lead by NiPS



## ICT 2010 :: Networking sessions

### Energy efficient ICT: toward zero-power devices for a greener planet

#### Technical description

Web site: <http://www.nipslab.org>

Coordinator: Luca GAMMAITONI (Universita' di Perugia, NIPS Laboratory - Physics Department, Italy)

#### Links and Documents

- "Disruptive Solutions for Energy Efficient ICT" FET Proactive Expert Consultation, Brussels Feb. 8-9 2010
- Energy Conversion: From Nanomachines to Renewable Sources - Int. Conference, 7-11 June 2010
- Micro Power Sources
- MicroEnergy day during the EU Sustainable Energy Week 2010
- NANOPOWER
- Shaping Future FET Proactive Initiatives
- Summer School: Energy Harvesting at micro and nanoscale, Aug. 1-6, 2010
- ZEROPOWER Coordinated Action proposal

## Networking session at ICT2010

[http://ec.europa.eu/information\\_society/events/cf/ict2010/item-display.cfm?id=3440](http://ec.europa.eu/information_society/events/cf/ict2010/item-display.cfm?id=3440)



# EH related initiatives

## Vibration Energy harvesting

3 partners: UNICT, UNIBR, NiPS  
Funded by PRIN (IT)  
0.2 M€, 1 year, lead by UNICT



*Laboratoire d'Electronique et de  
Technologies de l'Information*

2 partners: CEA-LETI (Fr), NiPS  
Self funded



Novel techniques and methods for the realization of energy harvesting systems capable of substituting/integrating existing batteries for the powering of autonomous electronic devices.

Proposal submitted to ONRG-US Navy

Aug. 1-8  
2010

# Summer School and International Workshop

Energy Harvesting at micro and nanoscale  
Noise in dynamical systems at the micro and nanoscale

**NiPS** Laboratory  
Noise in Physical Systems



**La Tenuta dei Ciclamini  
Avigliano Umbro (TR) - Italy**

[www.nipslab.org/summerschool](http://www.nipslab.org/summerschool)

**WISEPOWER**

**NANOPOWER**